



Cavity QED with atoms and ions

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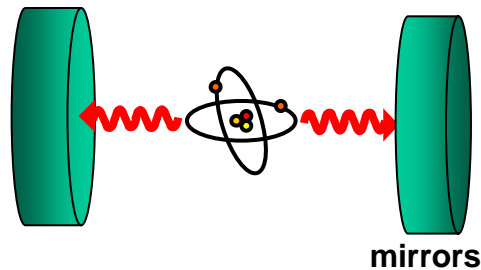
School of Physics

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Cavity QED

1 atom + 1 photon



entanglements

atom-photon

photon-photon

atom-atom

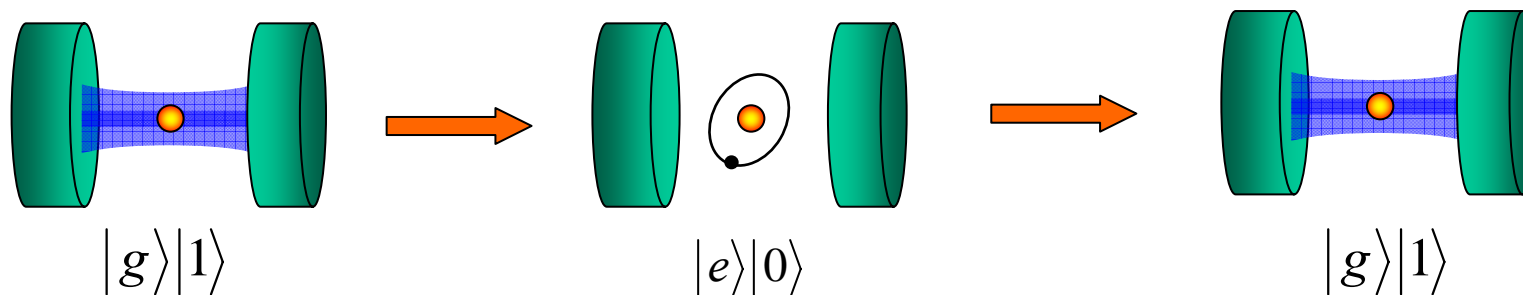
$$\begin{array}{cc}
 \vdots & \\
 \text{---} |e\rangle & \text{---} |1\rangle \\
 & \otimes \\
 \text{---} |g\rangle & \text{---} |0\rangle \\
 \text{atom} & \text{cavity}
 \end{array}$$

$$H_{\text{int}} = \hbar g_0(\vec{r}) [a^\dagger \sigma_- + a \sigma_+]$$

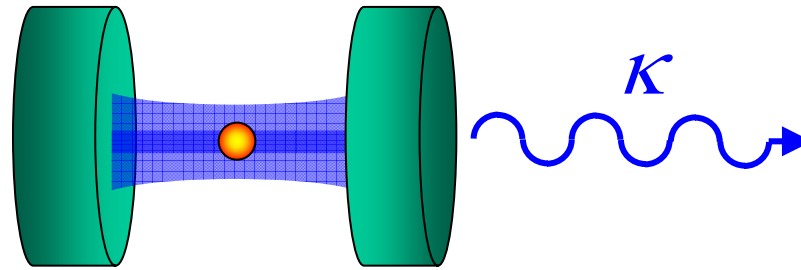
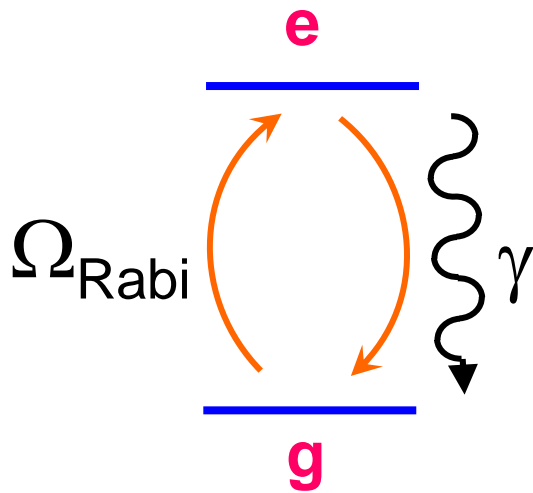
$$|00\rangle = |g\rangle|0\rangle$$

$$|\pm\rangle = \frac{1}{\sqrt{2}} (|g\rangle|1\rangle \pm |e\rangle|0\rangle)$$

Reversible, coherent ‘spontaneous’ emission (single photon Rabi flopping)



Cavity QED in the strong coupling regime— Rabi flopping with a **single photon**



Single photon Rabi frequency

$$g_0 \equiv \Omega_{\text{Rabi}}(1 \text{ photon}) = \gamma \sqrt{I(1 \text{ photon})/I_{\text{sat}}}$$

$I(1 \text{ photon})$ — **intensity for 1 photon in cavity**

I_{sat} — **saturation intensity**

coherent Rabi flopping requires :

$$g_0 > \gamma \quad \text{hence} \quad I(1 \text{ photon}) > I_{\text{sat}}$$

$$g_0 > K$$

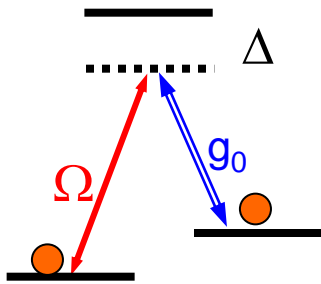
Cavity QED

Coherent coupling of matter qubits (e.g. single atoms) and photonic qubits

- **Entanglement generation**
 - Atom-photon
 - Photon-photon
 - Atom-atom
- **Quantum communication**
 - Atoms are good material qubits
 - Photons travel well
 - CQED provides connection
- **Cavities make good single atom detectors**

Estimating the success rate

Off-resonant Raman transition using cavity field



$$\Omega_{\text{effective}} = \frac{\Omega g_0}{2\Delta}$$

effective Rabi frequency

$$\Gamma_{\text{effective}} = \gamma \left(\frac{\Omega g_0}{4\Delta^2} \right)$$

effective spontaneous emission rate

Coherence requires $\Omega_{\text{effective}} \gg \Gamma_{\text{effective}}$ and $\Omega_{\text{effective}} \gg \kappa$

or

$$\frac{g_0^2}{\kappa\gamma} \gg 1 \quad \text{and} \quad g_0 \gg \kappa$$

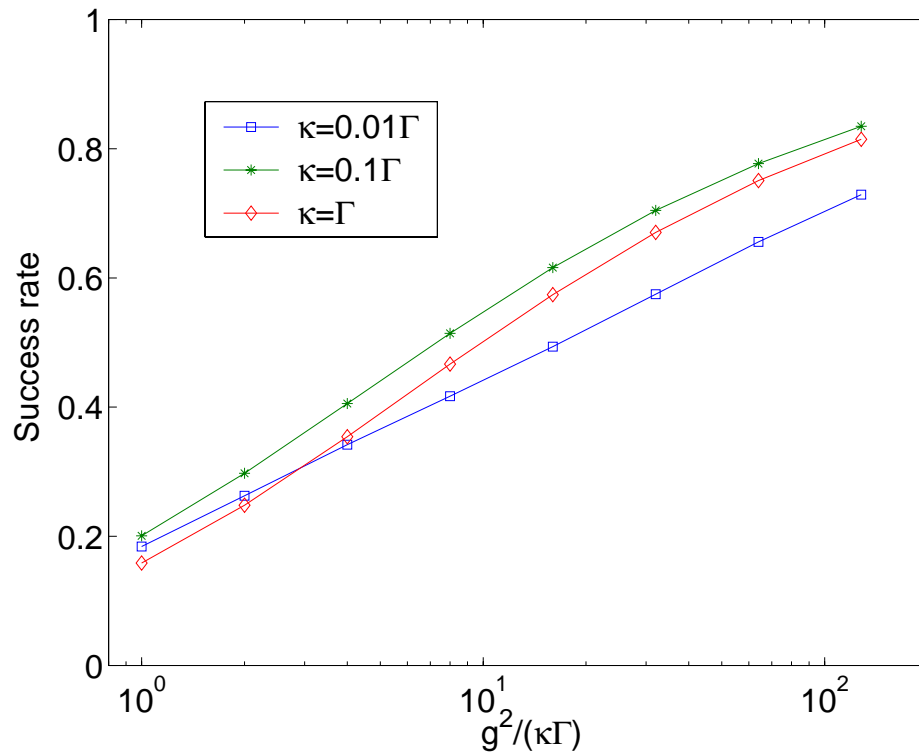
$\frac{g_0^2}{\kappa\gamma}$ is the atom cooperativity parameter

Success rate:

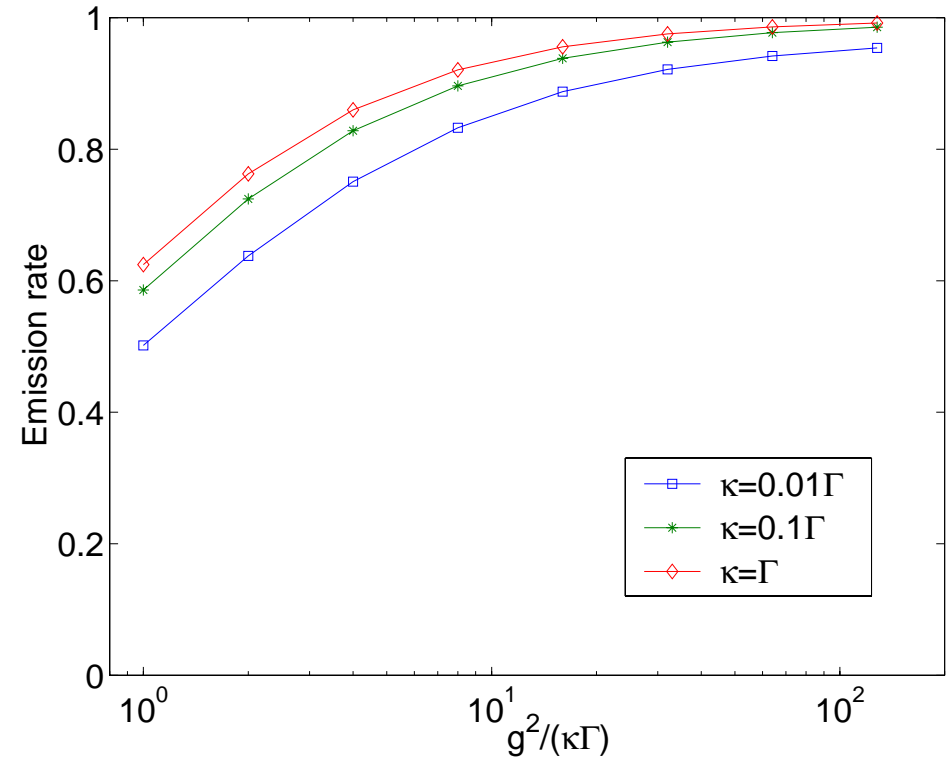
$$S_{\text{optimal}} = 1 - 2 \frac{\sqrt{\kappa\gamma}}{g_0}$$

Performance

State transfer (element of gate)



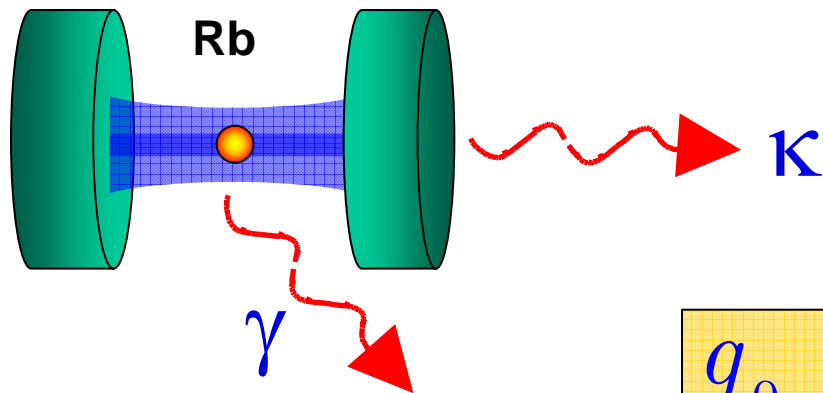
Single photon generator



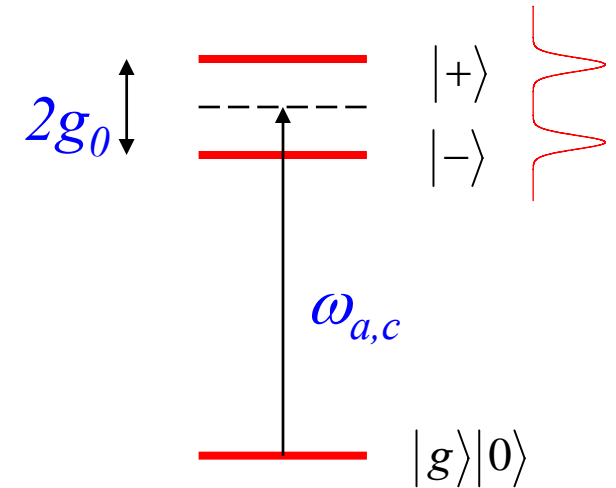
calculations by Li You

Conditional fidelities > 99% possible with cavity emission detection

Strong coupling



$$g_0 > \gamma, \kappa$$



$$g_0 = \vec{d} \cdot \vec{E}_0 \propto V^{-1/2}$$

$$\kappa = \pi c / FL$$

$$g_0 = \sqrt{\frac{3c\lambda\gamma}{\pi\sqrt{2rL^3}}}$$

$$F = 2\pi / \delta$$

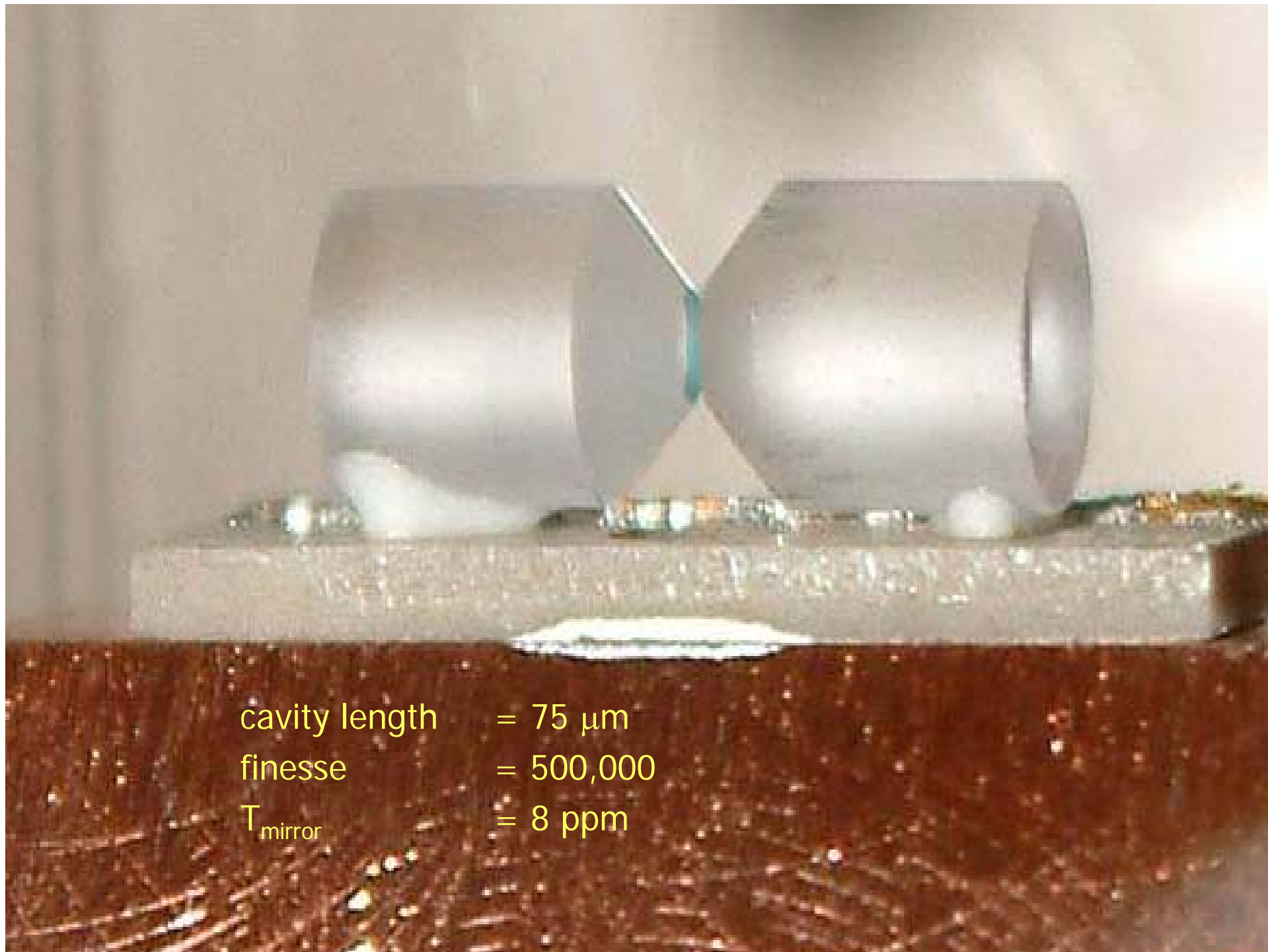
$$C_1 = \frac{g_0^2}{\gamma\kappa} = 51$$

γ – atomic decay rate
 r – mirror radius of curvature
 L – cavity length

$L < 1000 \mu\text{m}$ for strong transitions

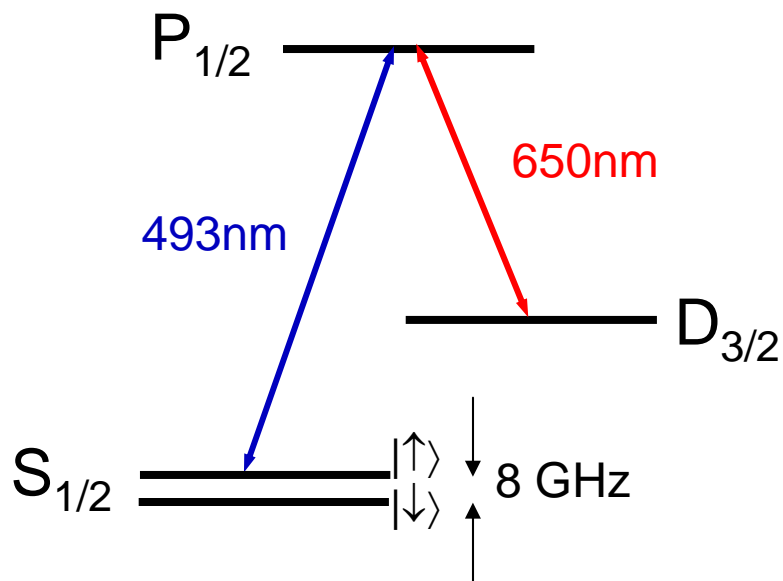
Finesse, $F > 100,000$ required for $g > \kappa$

$r > 1 \text{ cm}$ for super-polishing



cavity length = $75\ \mu\text{m}$
finesse = 500,000
 T_{mirror} = 8 ppm

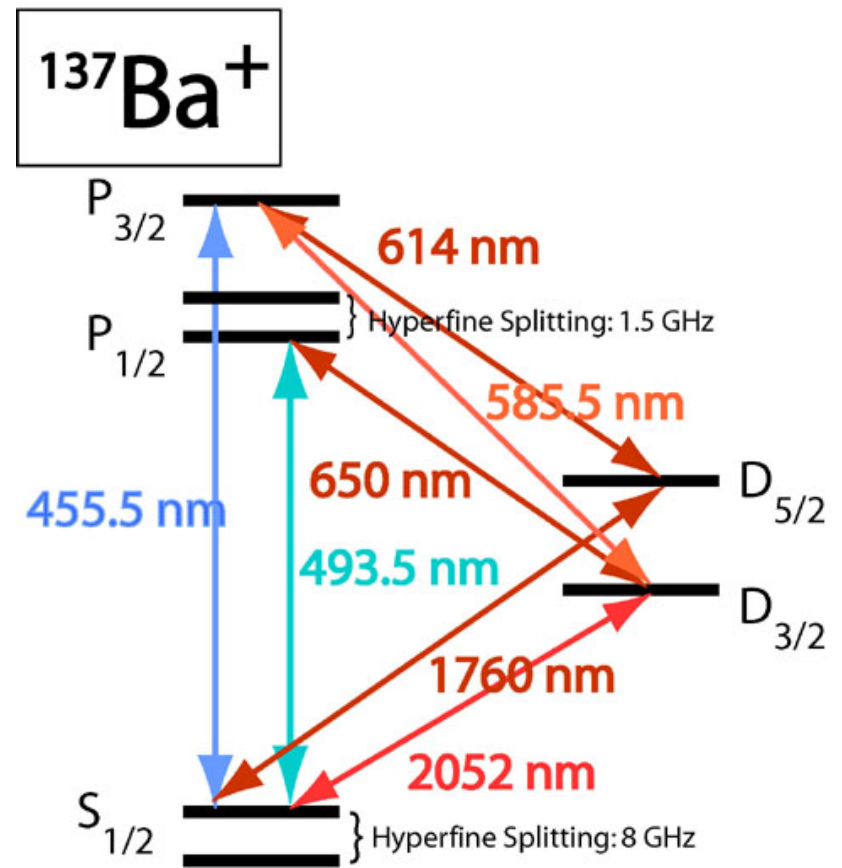
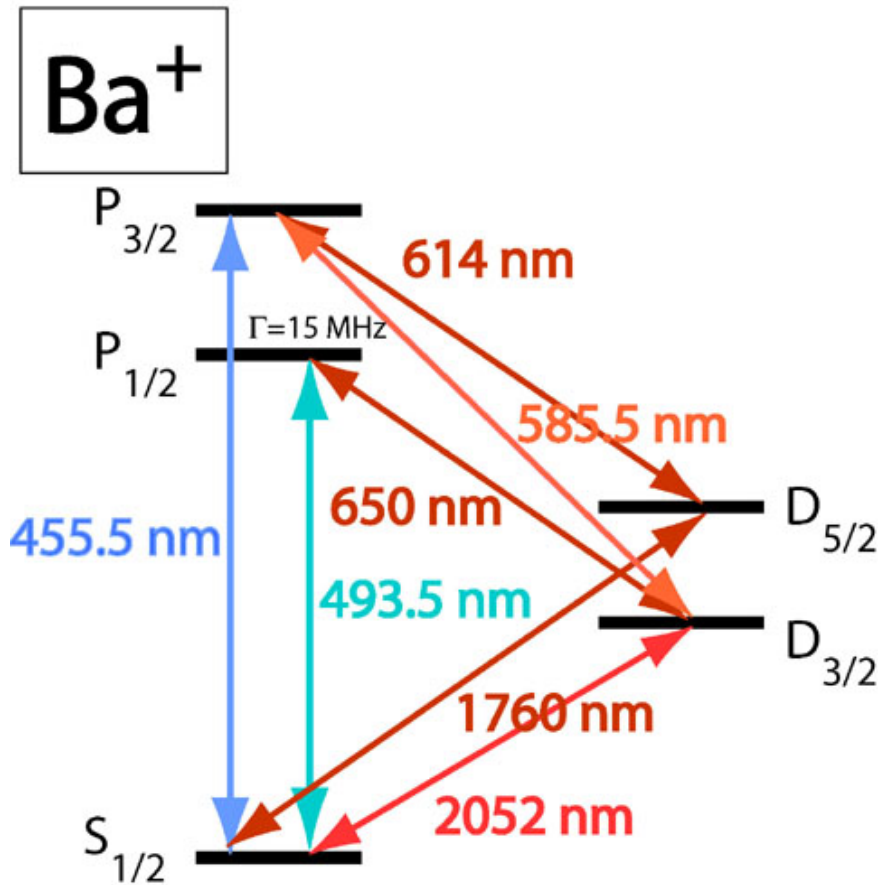
Trapped Ba⁺ Ion Cavity QED



Ba⁺ advantages:

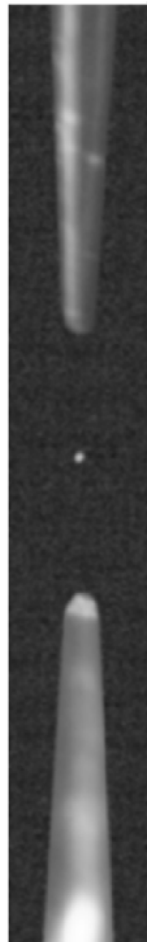
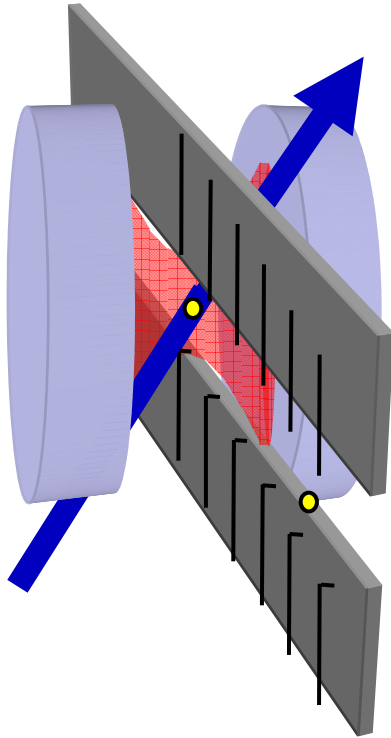
- Convenient lasers
- High finesse cavities possible on both blue and red transition
- Strong coupling regime possible with ~1 mm cavities

Relevant Ba⁺ levels



“borrowed” from Michigan ion trap database

Integration challenges

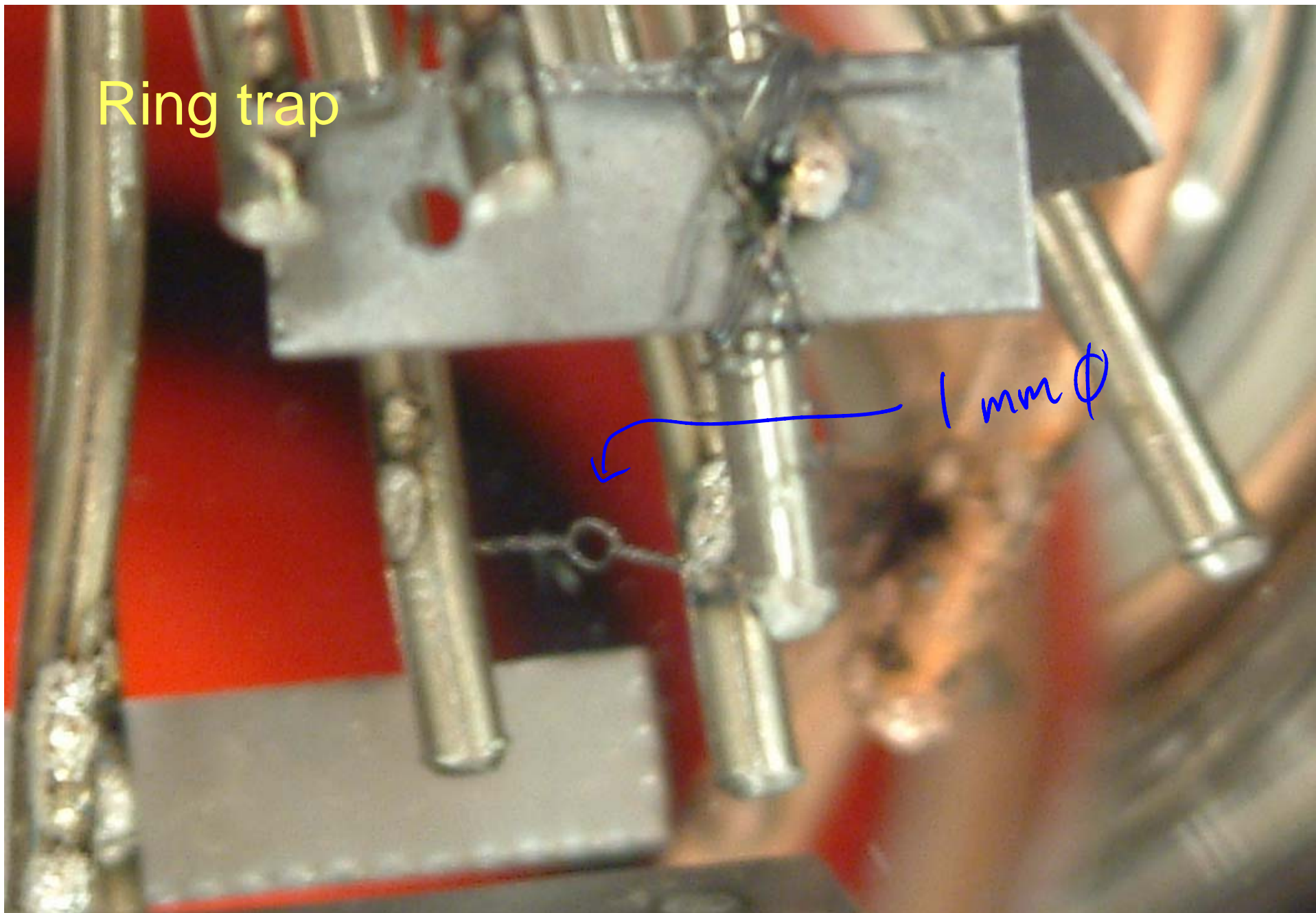


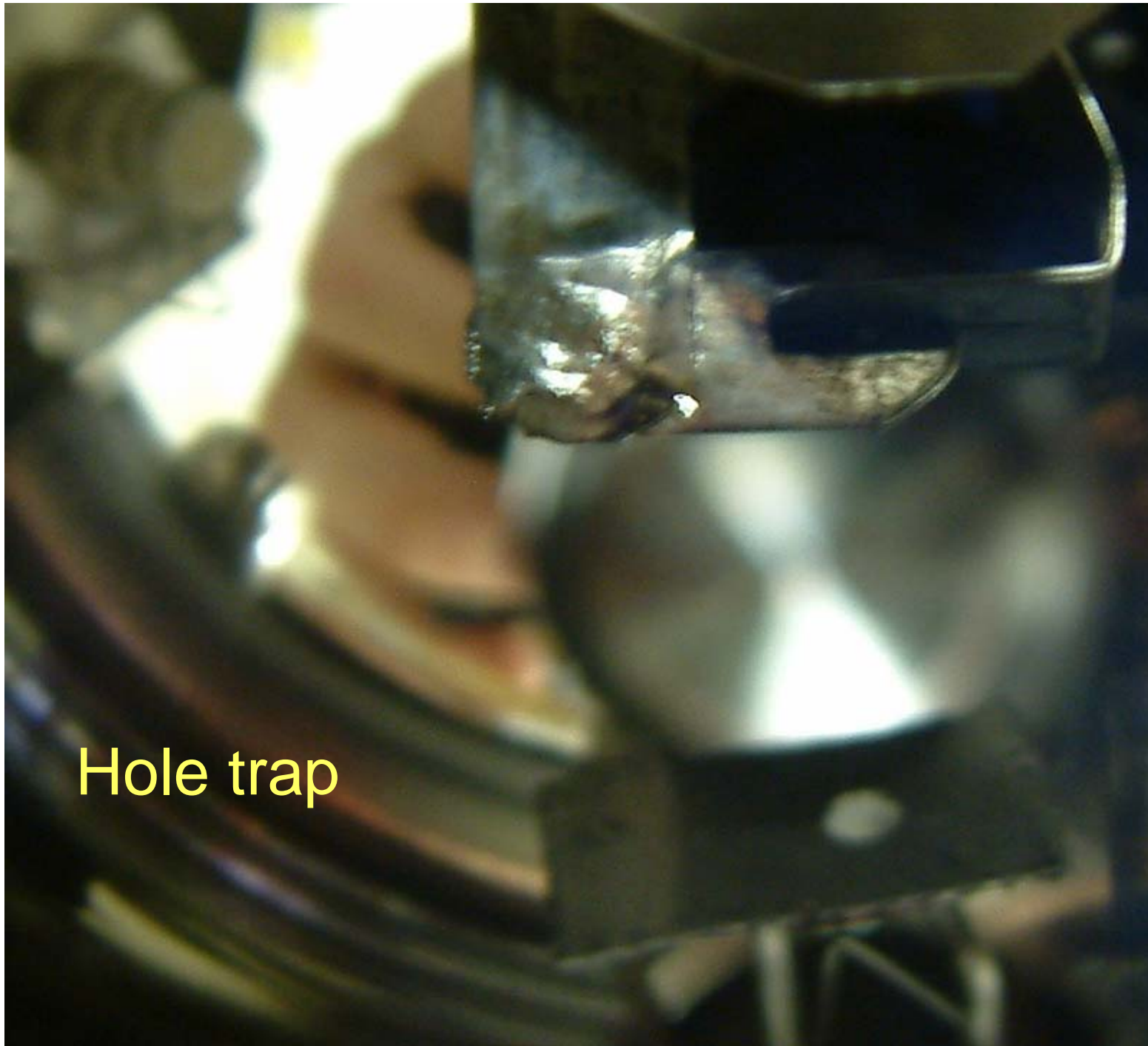
- Integrating small cavities with ion trap electrodes
- Minimizing charging of mirrors and effects of mirror dielectrics

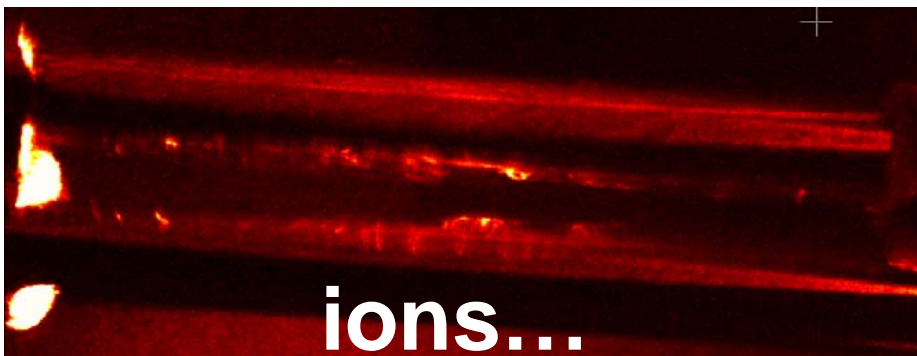
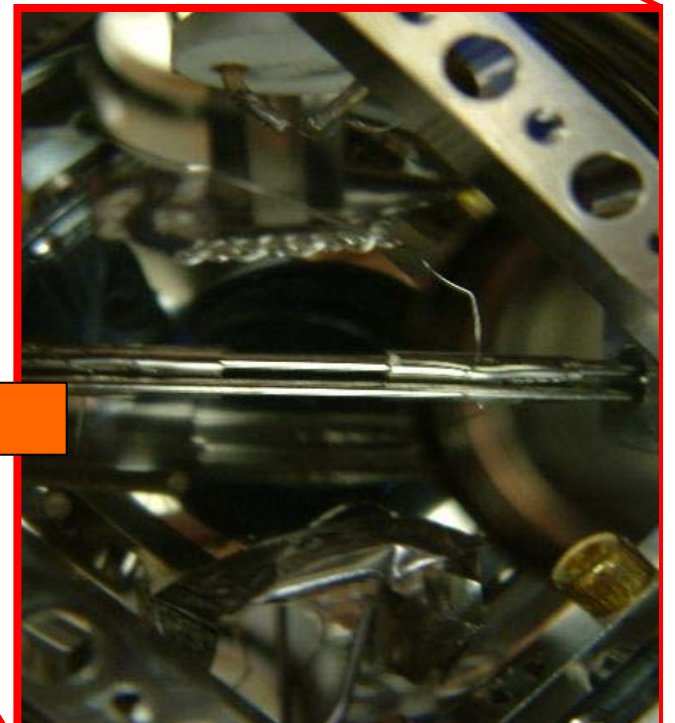
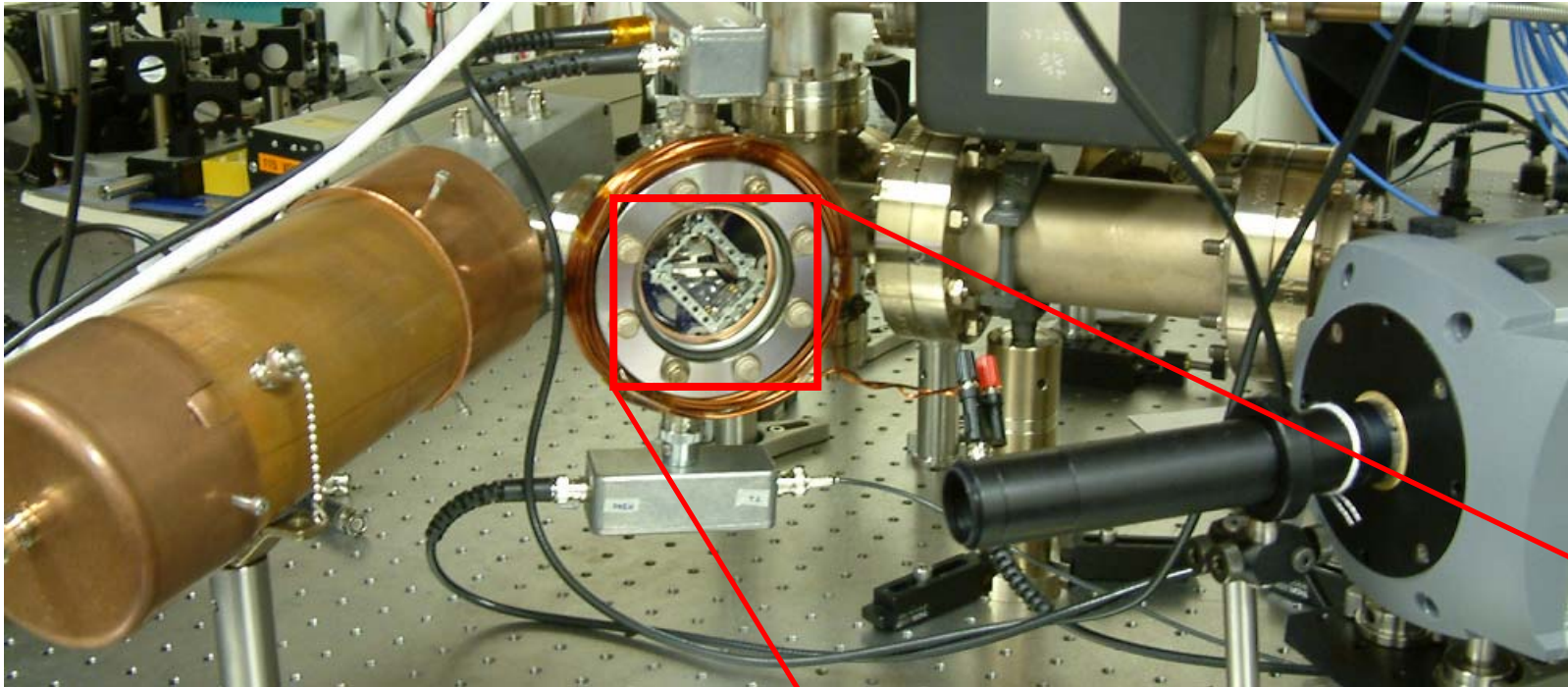
Possible micro-traps
(Michigan)

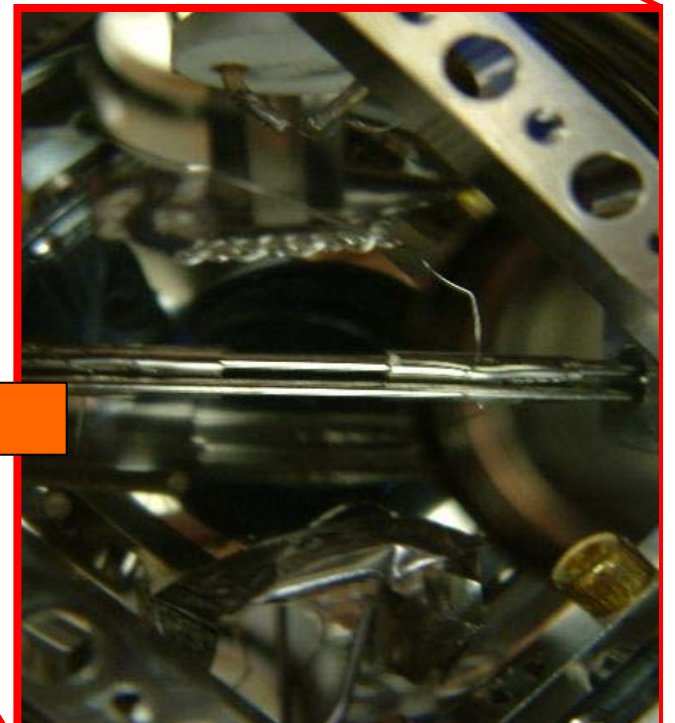
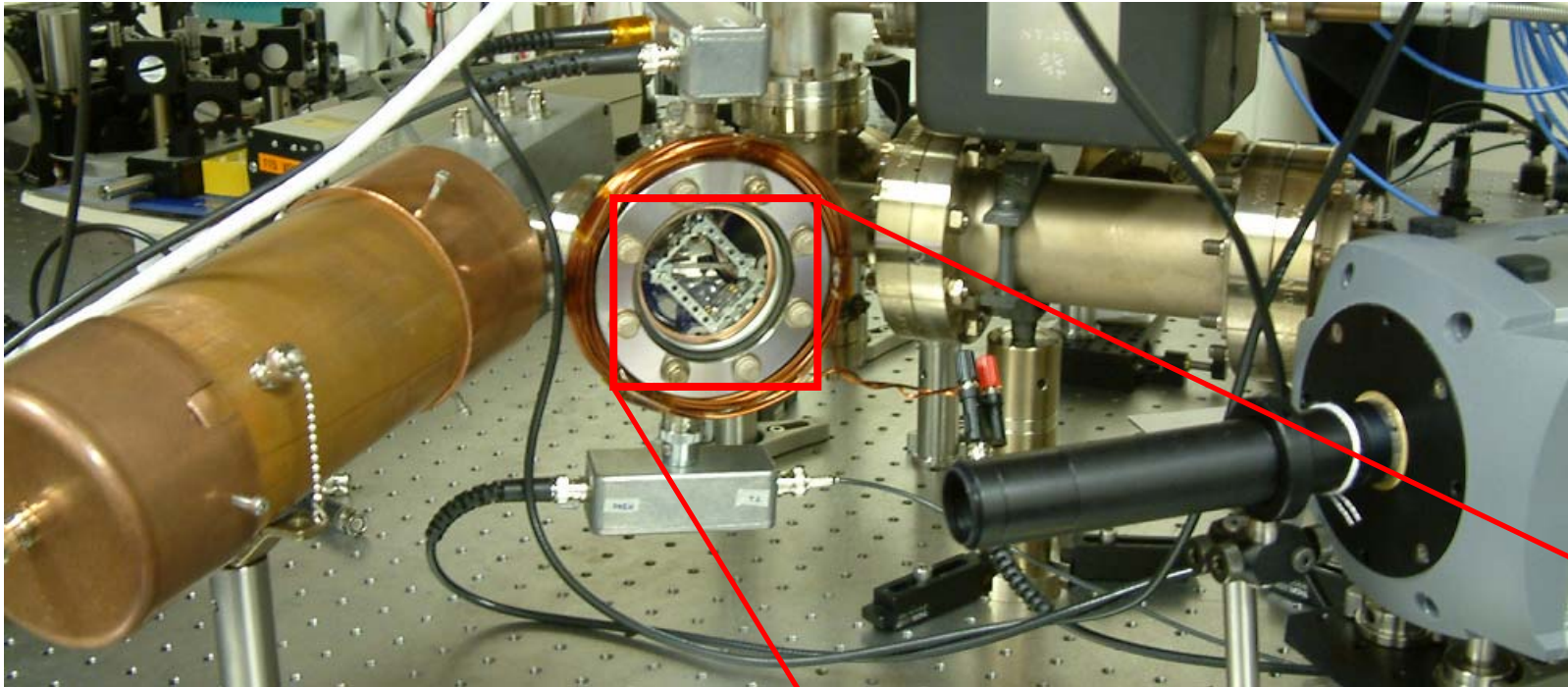
Ring trap

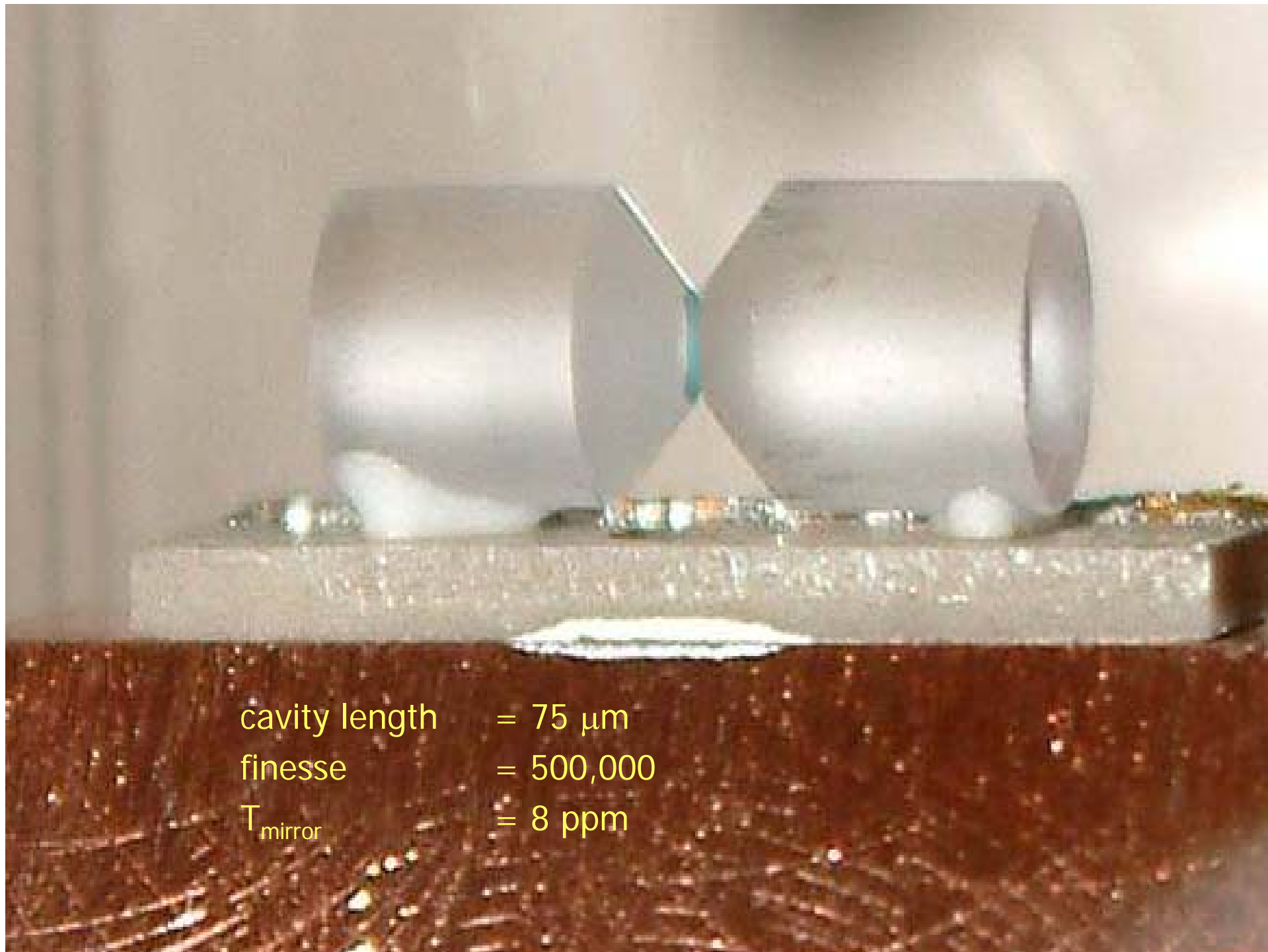
1 mm Φ



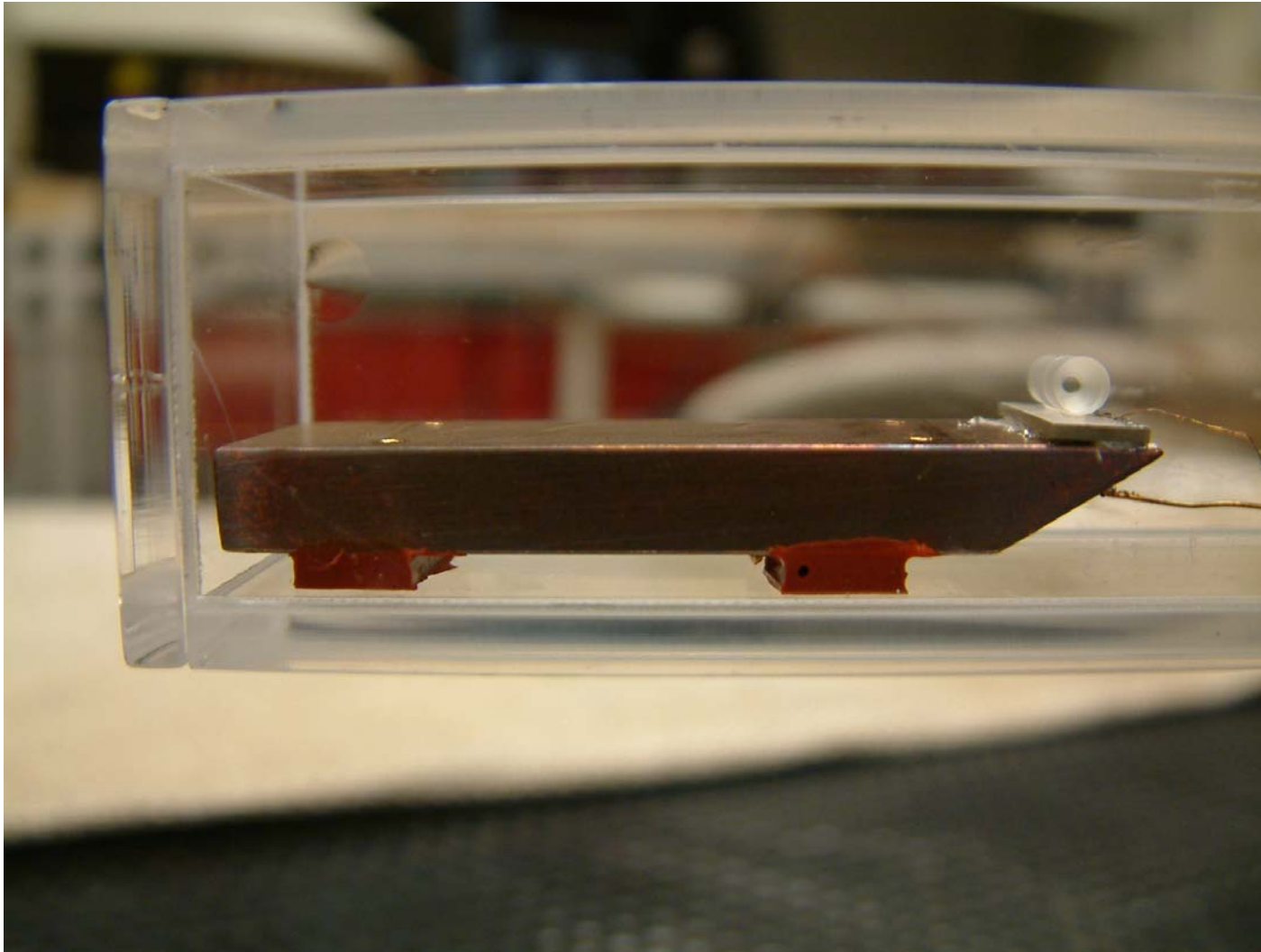








cavity length = $75\ \mu\text{m}$
finesse = 500,000
 T_{mirror} = 8 ppm



CAVITY 3

$$l = 221.5 \mu m$$

$$R = 2.5 cm$$

$$\frac{\kappa}{2\pi} = 5.73 MHz$$

$$\frac{g_0}{2\pi} = 17.7 MHz$$

$$\mathfrak{I} = 58,000$$

4ppm

100ppm

strong coupling regime

$$g_0 > (\kappa, \gamma)$$

1-sided Cavity

How to get an atom in the cavity

Atomic beams

Falling cold atoms

- single atom transits observed

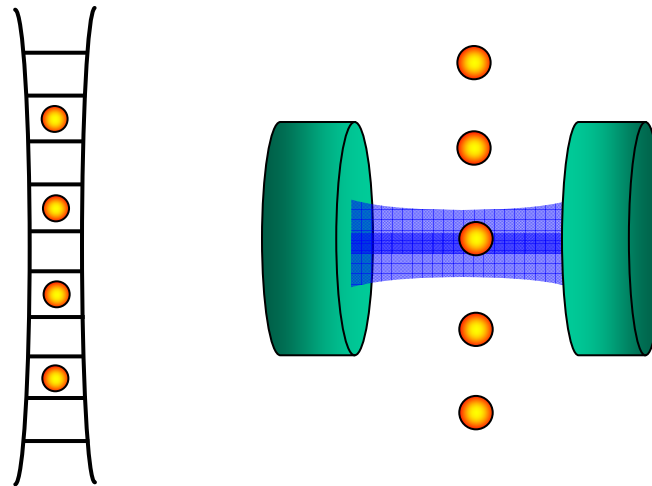
Catching the falling atoms

- trapping using the cavity modes

Trapping the atoms externally and transferring them into the cavity

Caltech
MPQ (Rempe)

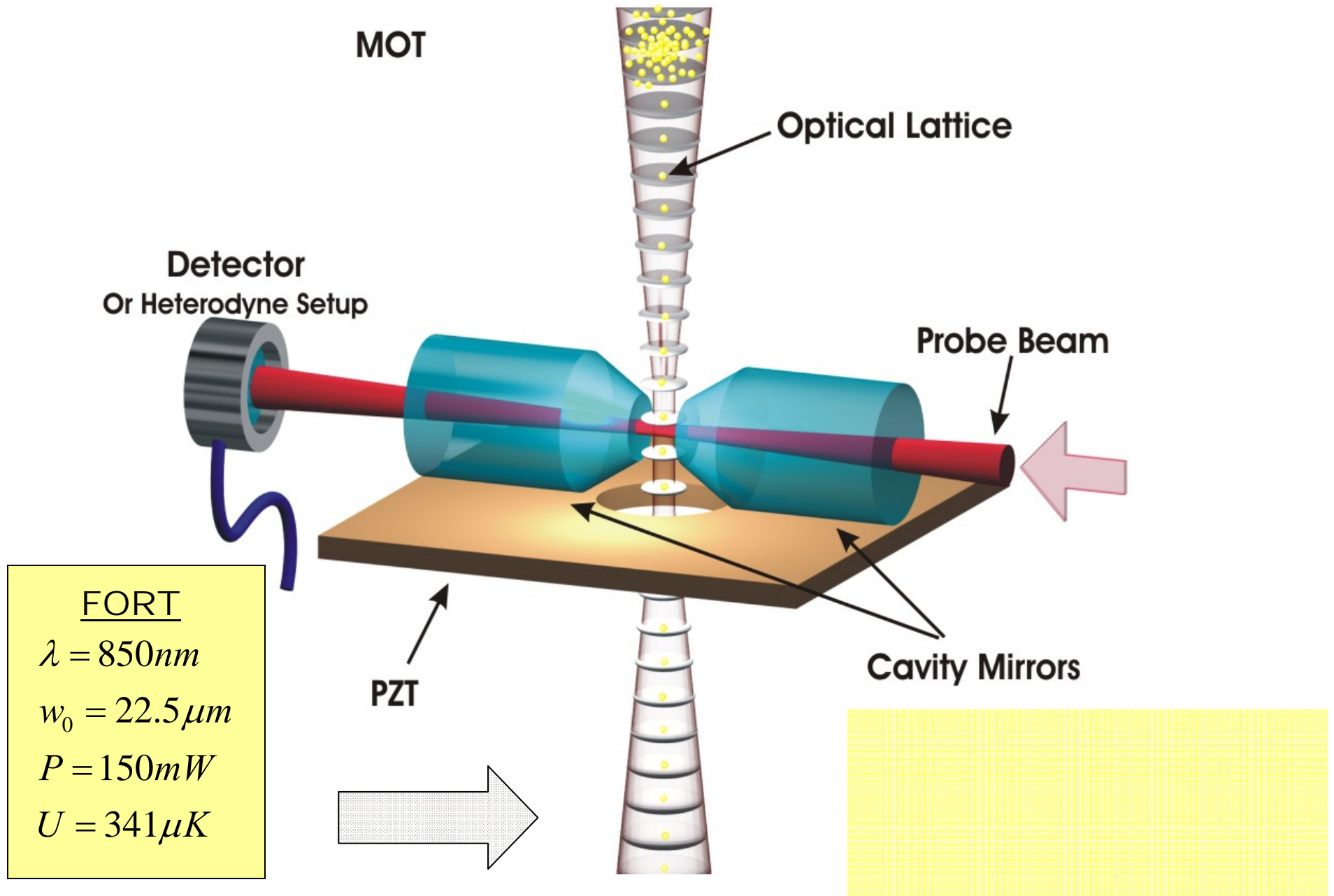
Georgia Tech
MPQ (Rempe)



also, single trapped ions

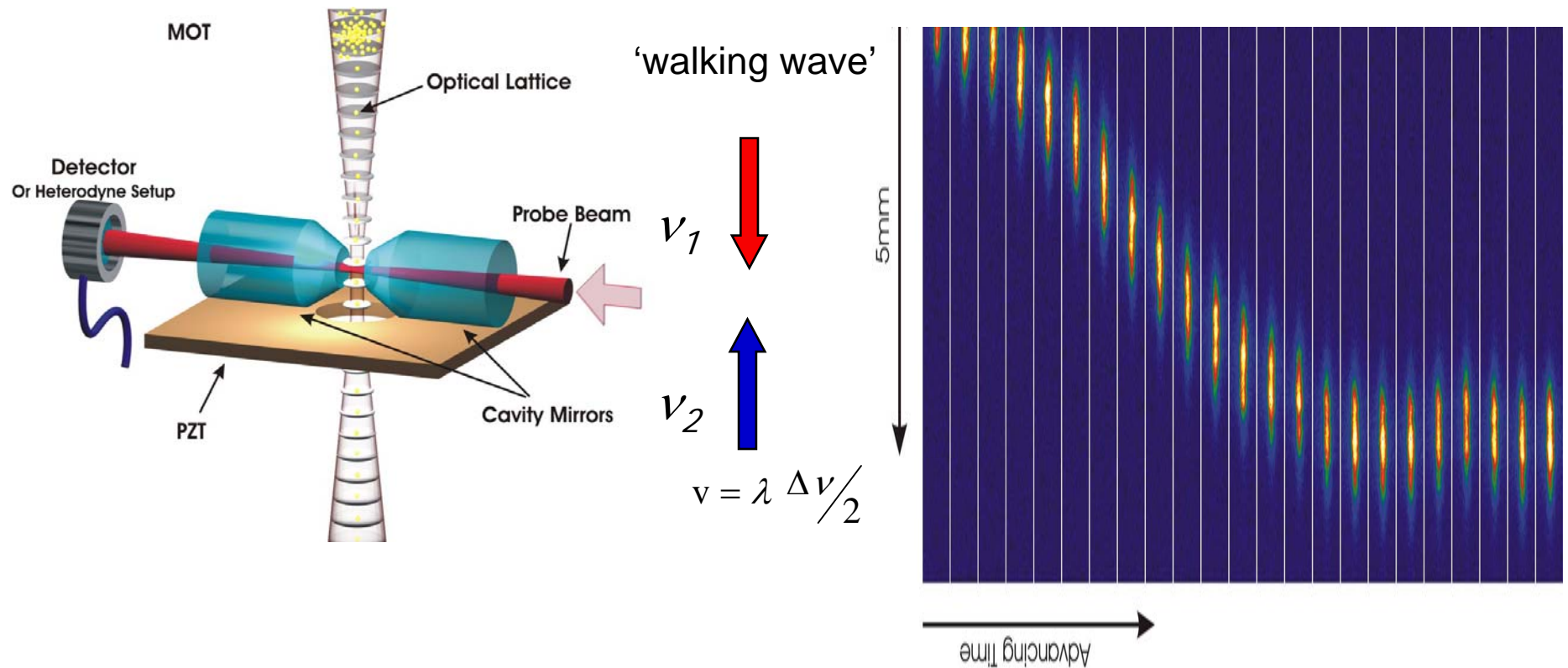
MPQ (Lange), Innsbruck

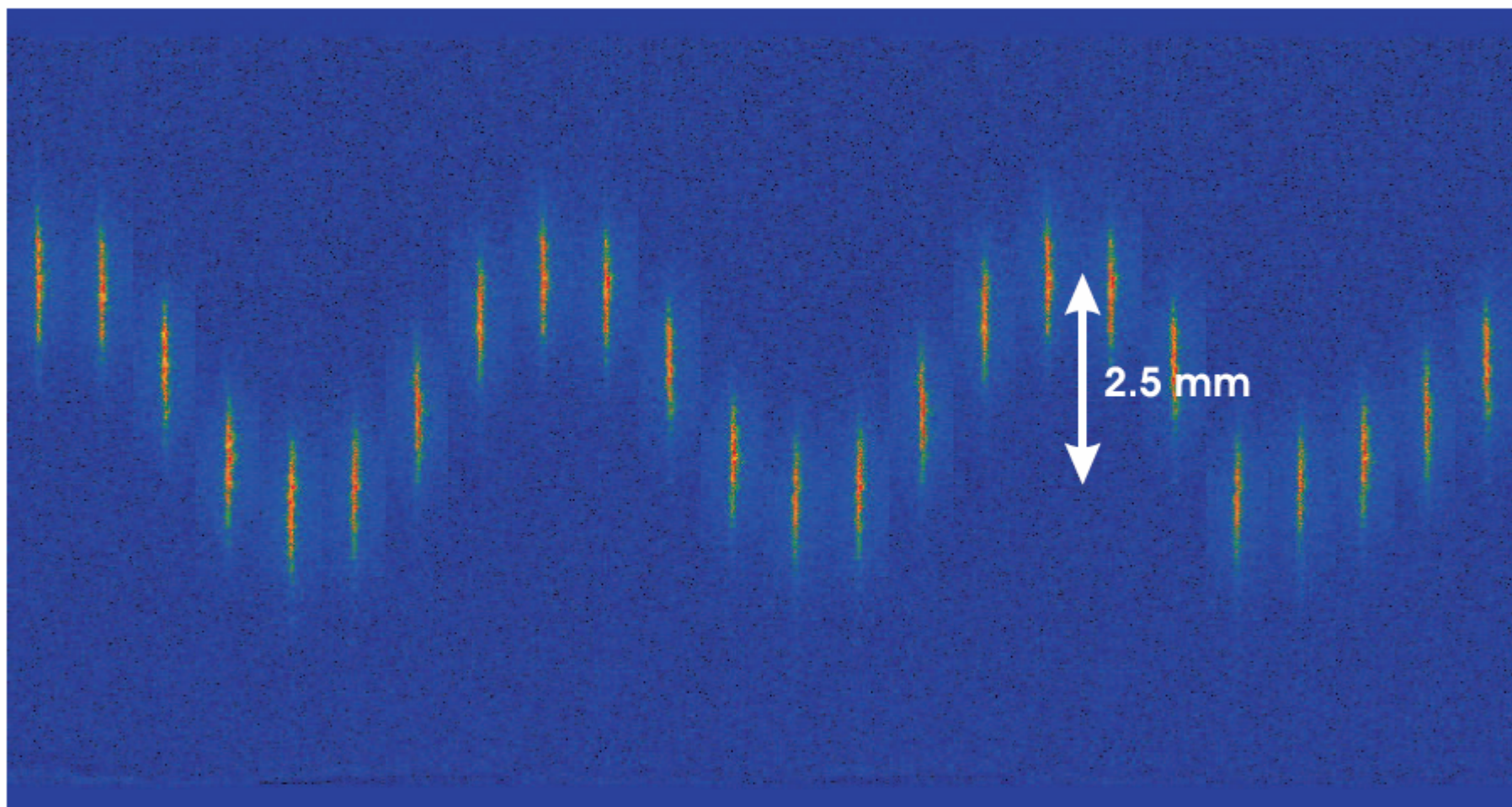
Our System



Neutral atom ^{87}Rb work

Optical Lattice

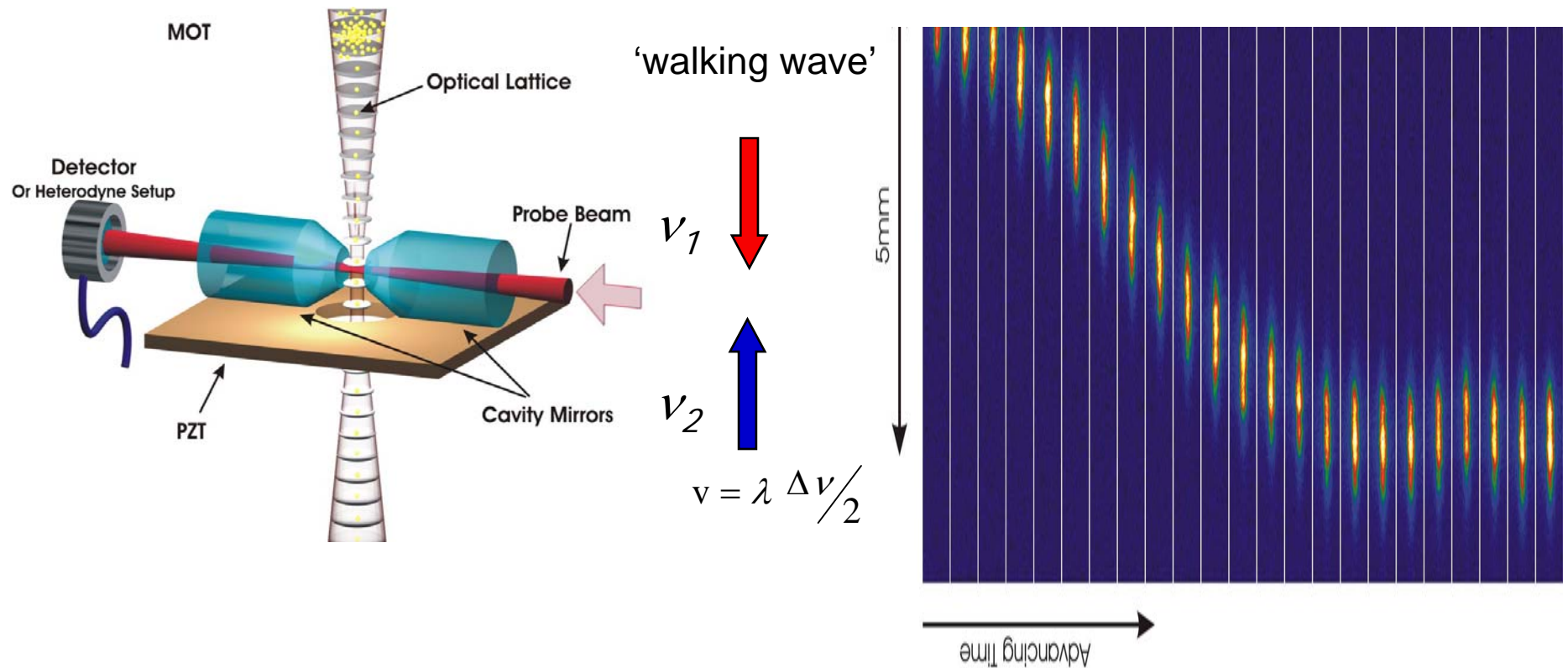


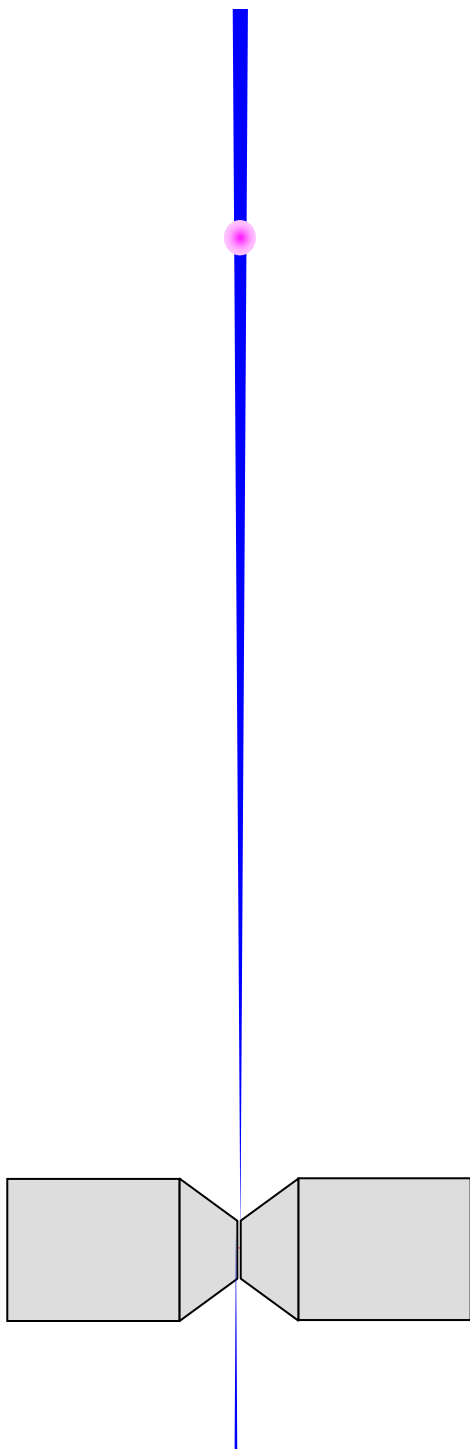


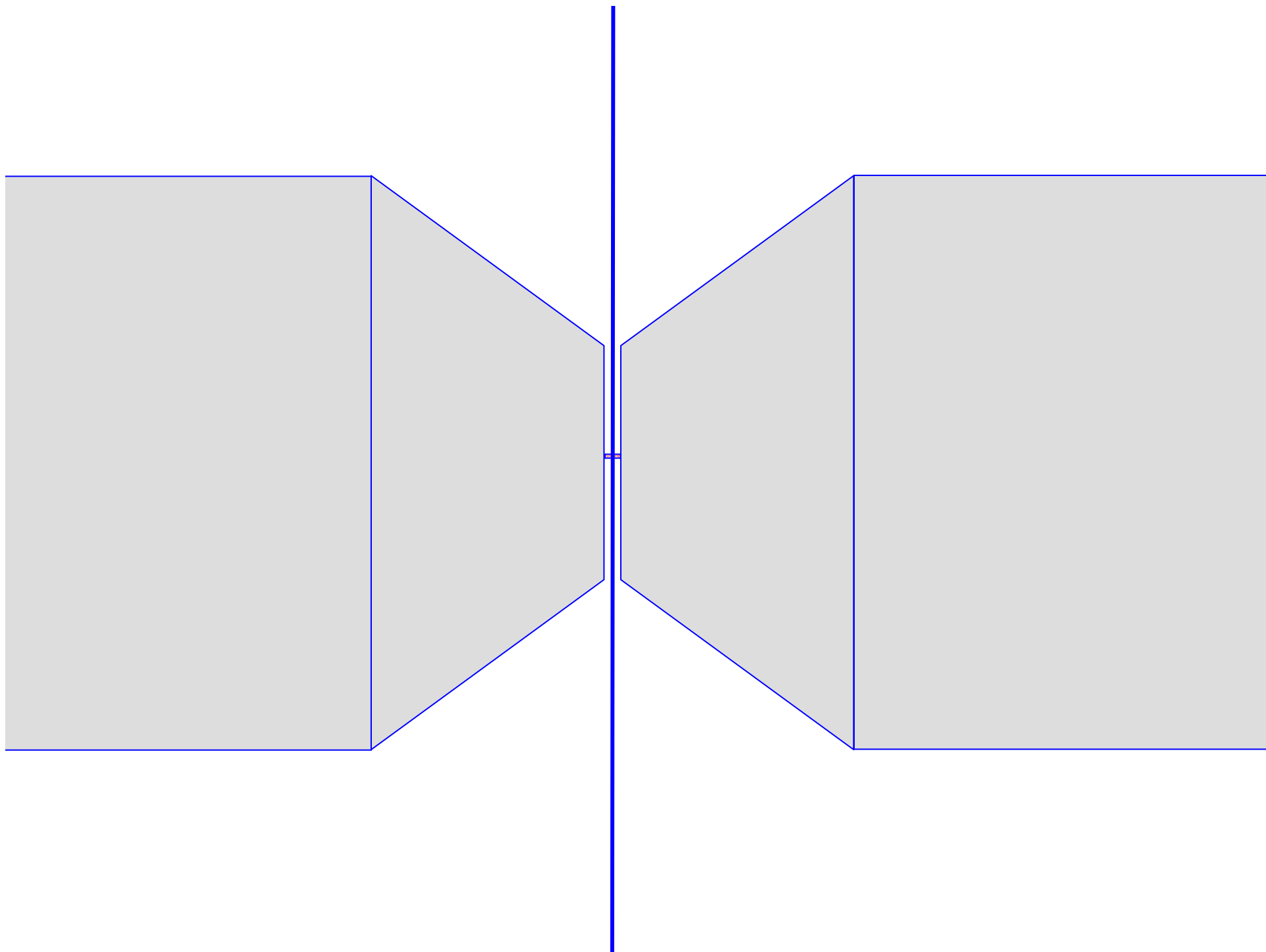
1 ms/frame

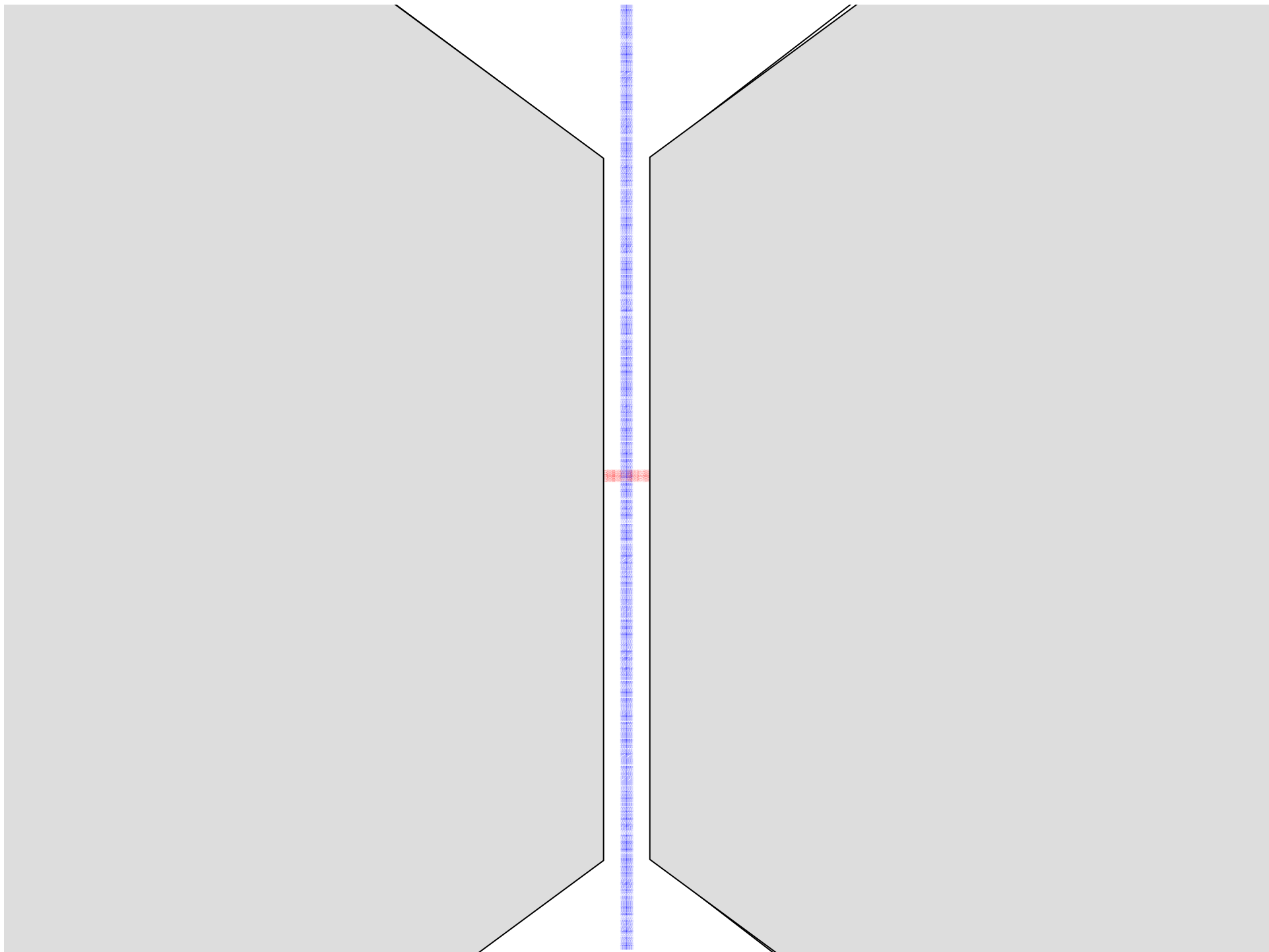
Neutral atom ^{87}Rb work

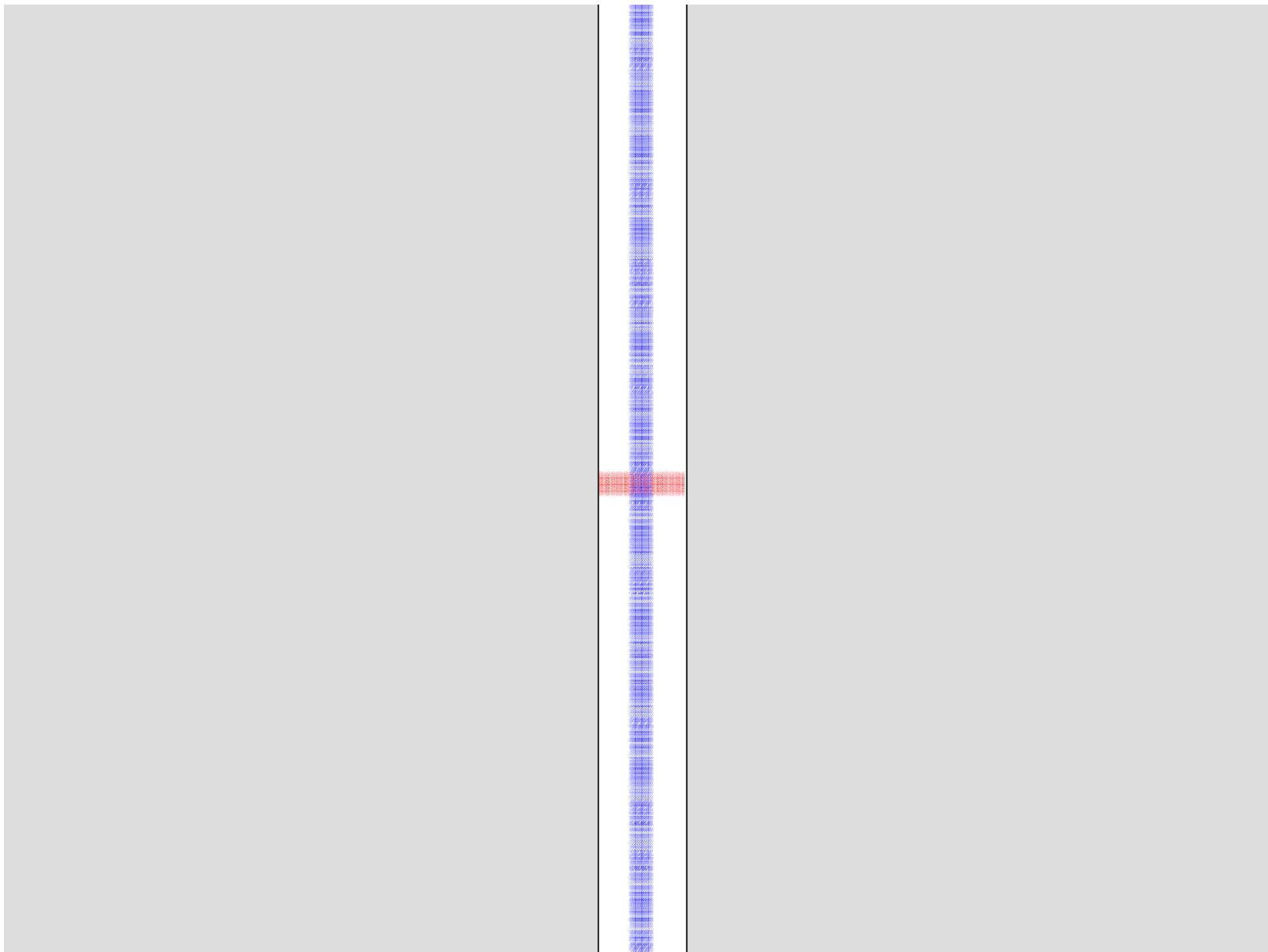
Optical Lattice

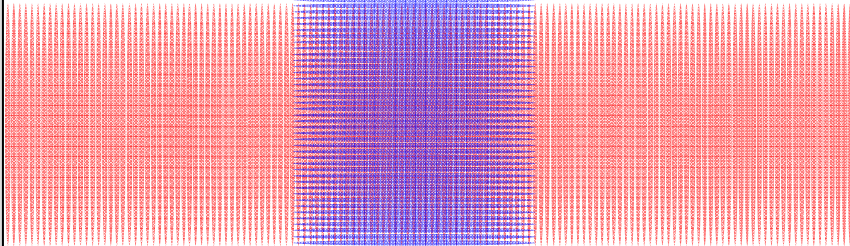
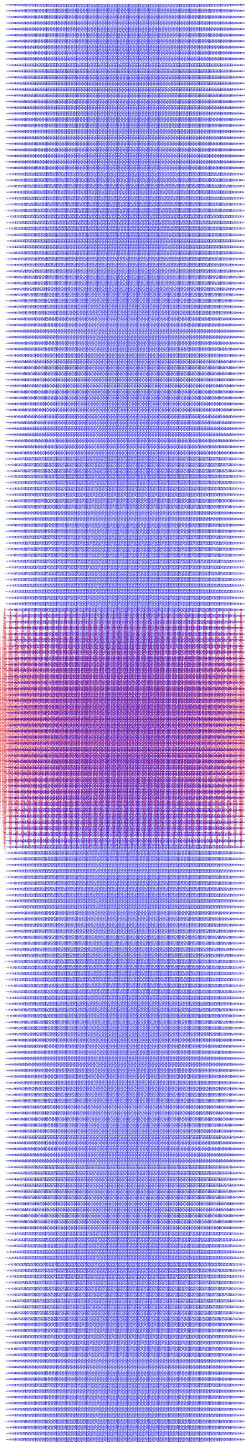


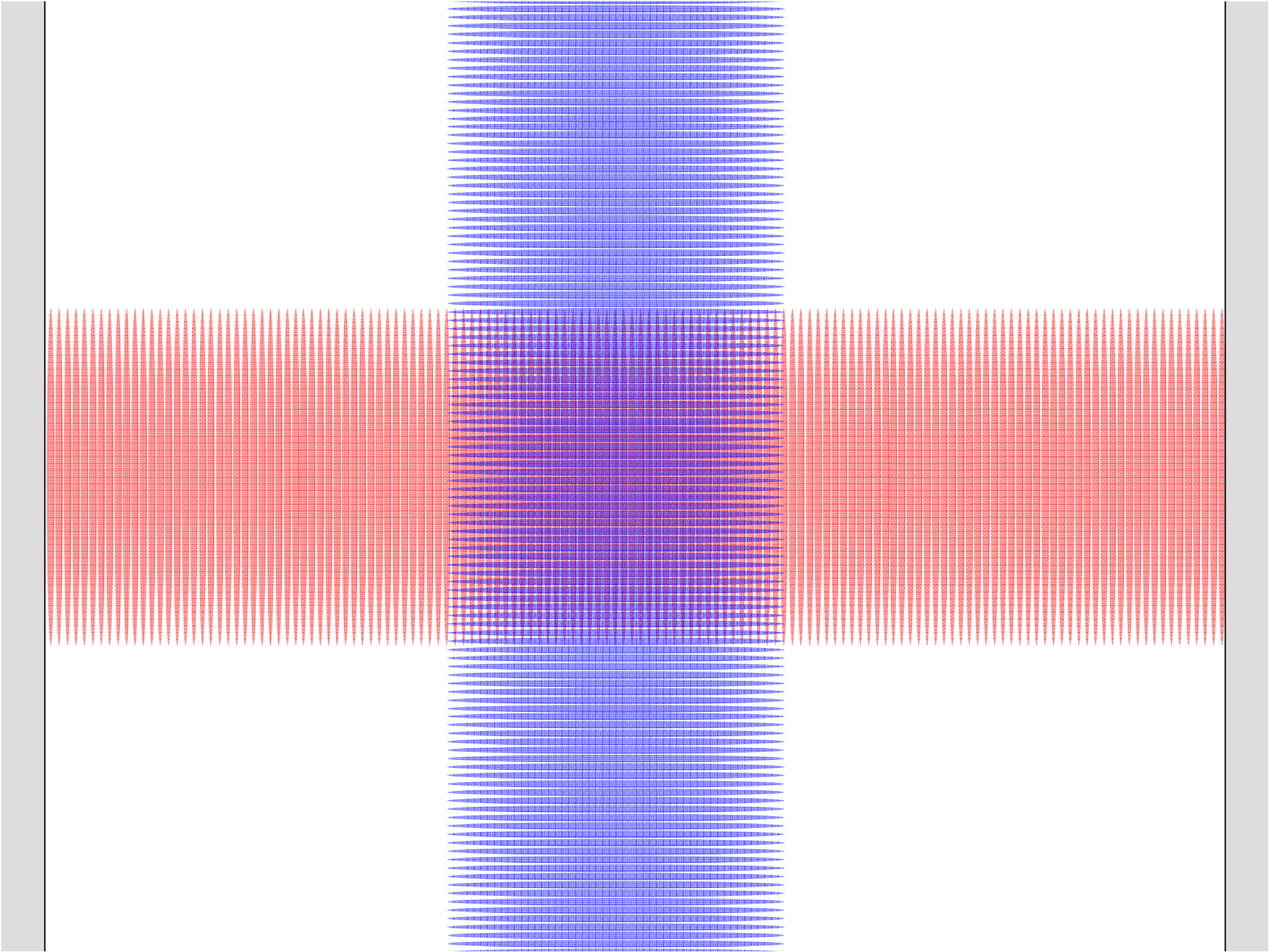




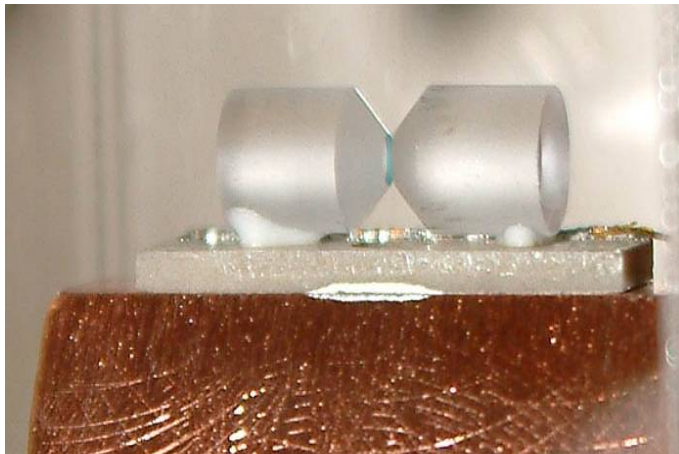




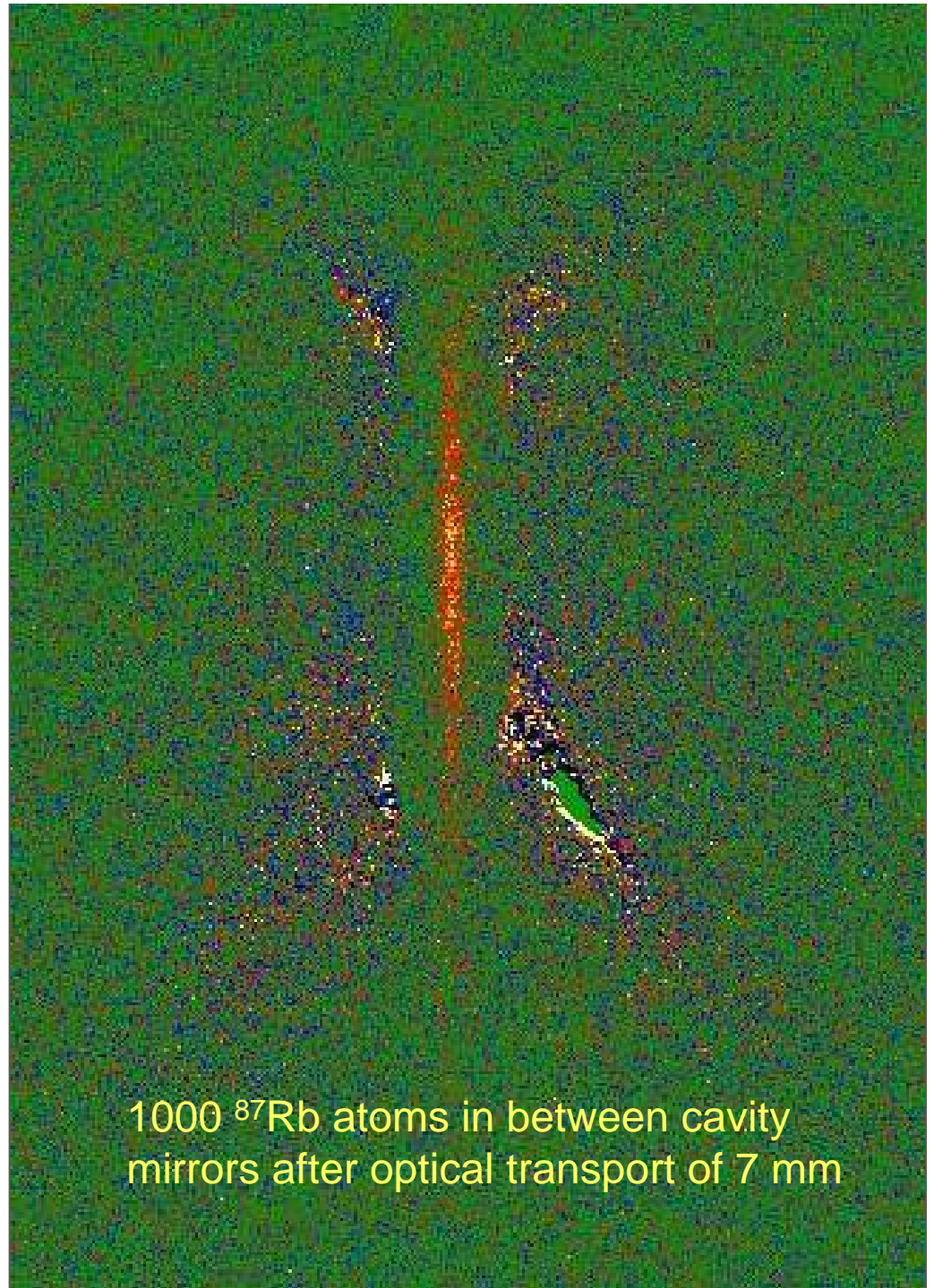




Improved Imaging allows us to image
atoms in the cavity

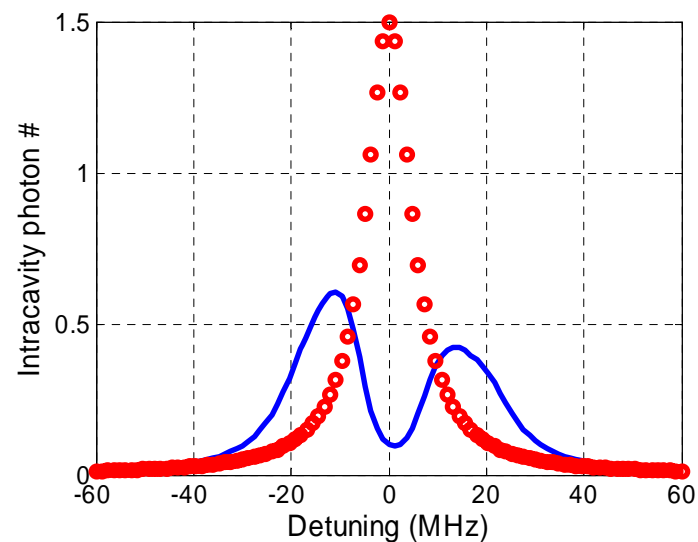
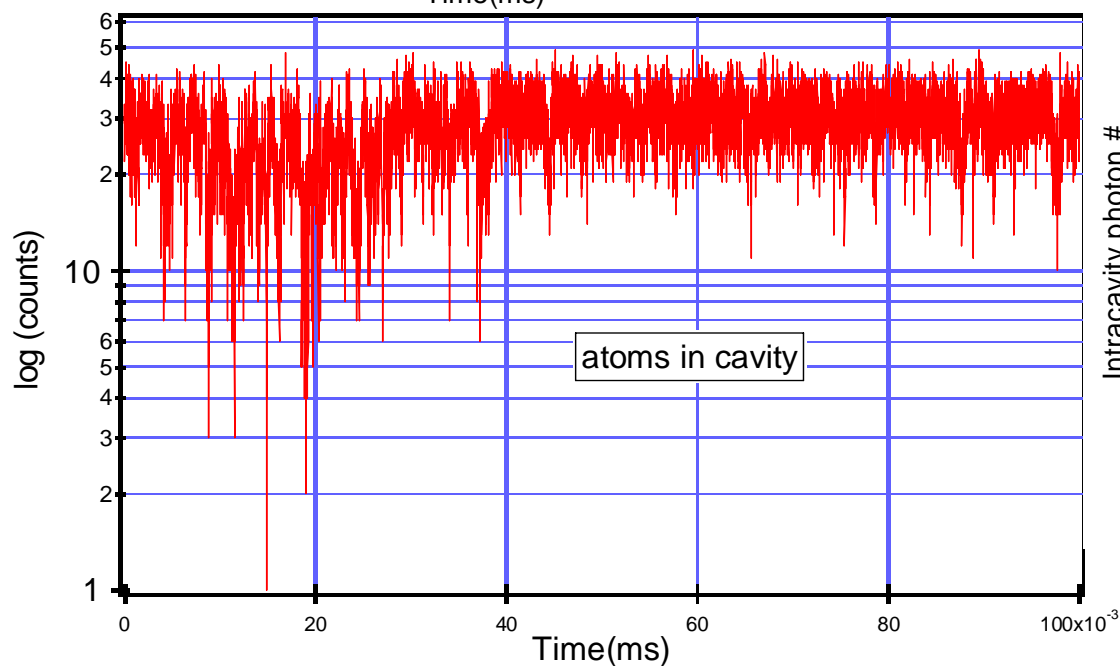
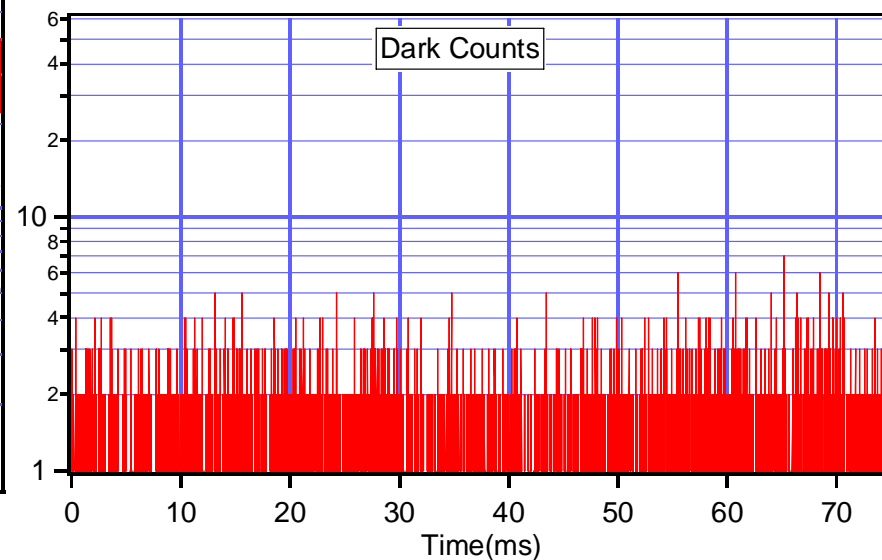
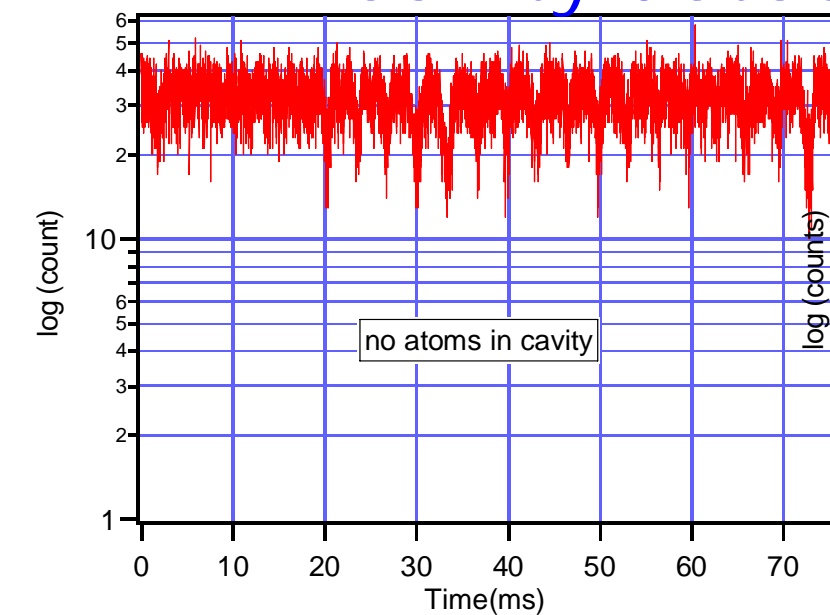


Mirror Separation = $225\ \mu\text{m}$



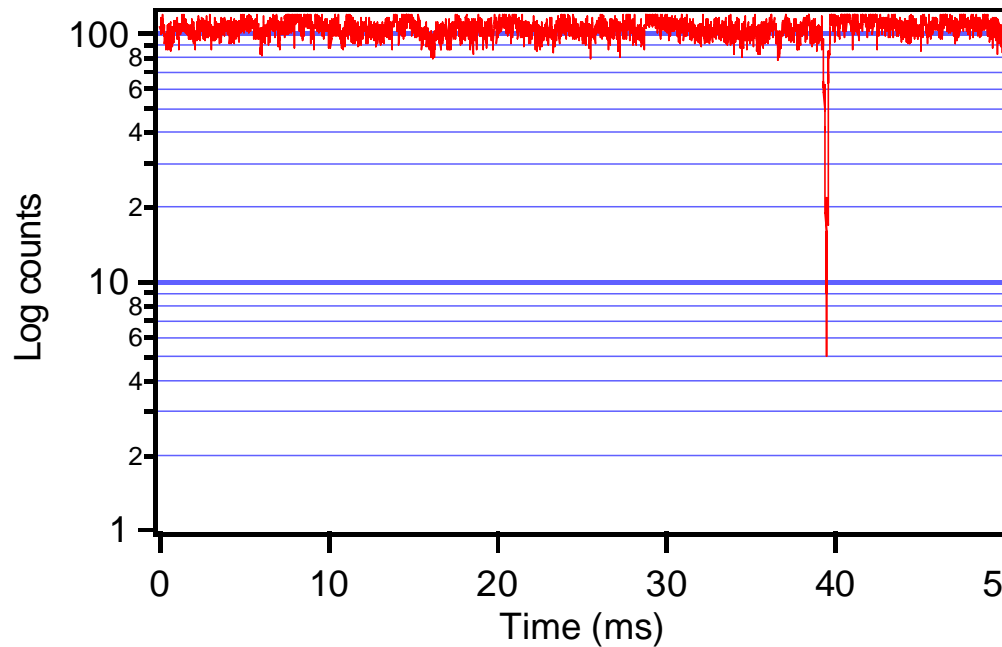
1000 ^{87}Rb atoms in between cavity
mirrors after optical transport of 7 mm

Cavity detection of atoms

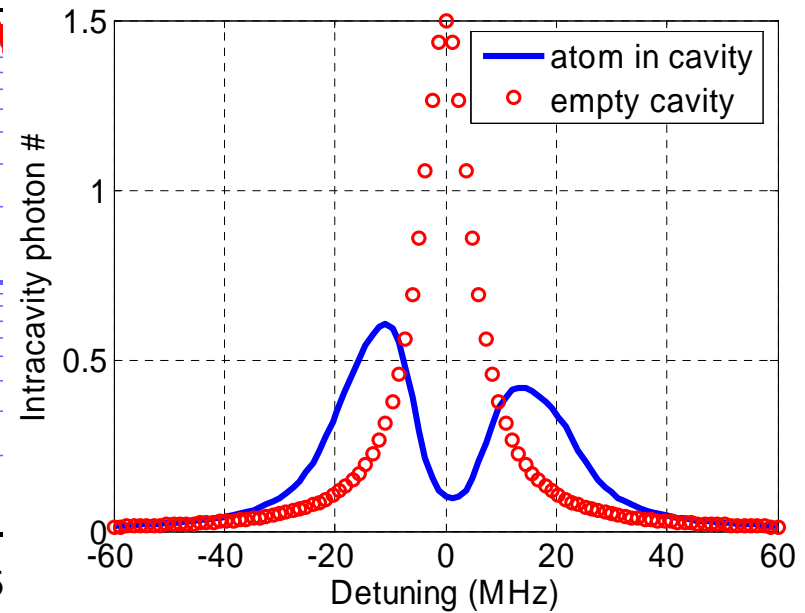


Theoretical plot
 $n=1.5$

Single atoms in cavity



Atoms entering cavity,
 $n=1.1$ photons



Theoretical plot for
 $n=1.1$

Improving the single atom signals

“distill” from many atoms to a single atom in cavity

- Intercavity cooling for “non-destructive” intercavity detection of atoms

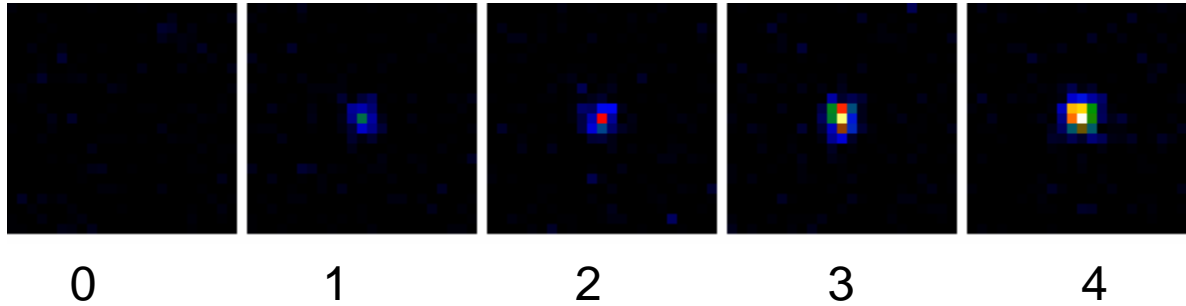
Recent progress: cavity signals extended from 10 ms to > 100 ms

Start with one atom in lattice

- Single atom magneto-optic trap (MOT)
- Transfer atoms into 1-D lattice optical dipole trap
- Continuous observation of atoms in lattice

A neutral atom quantum register!

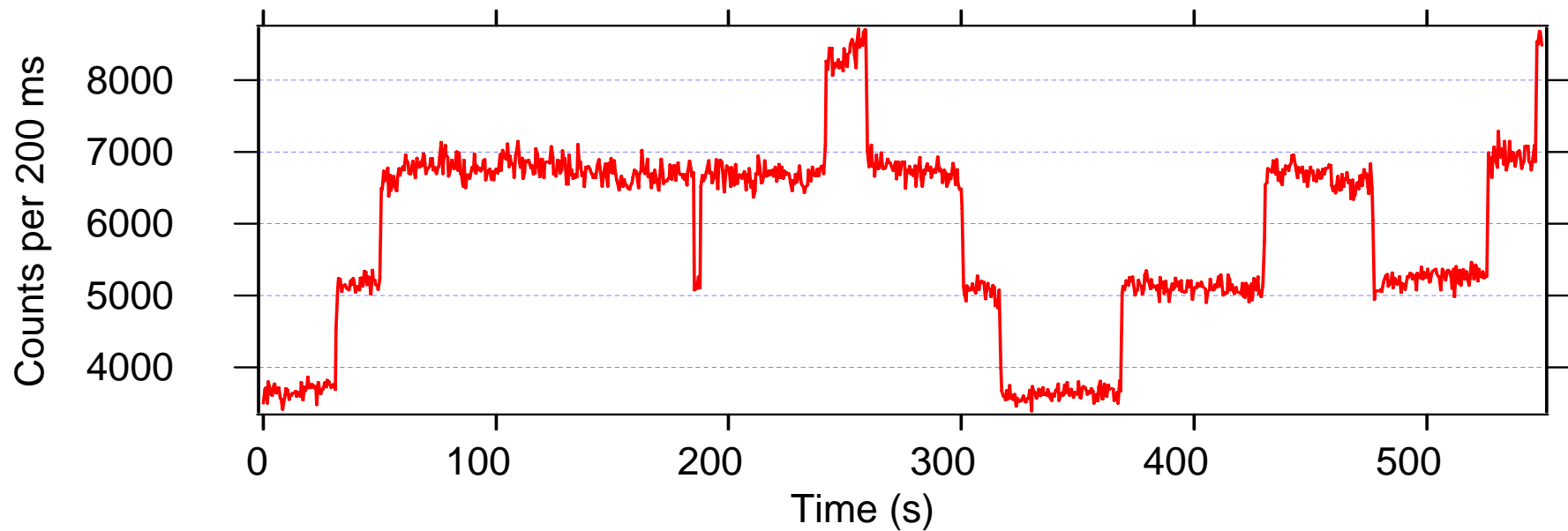
Single Atom MOT

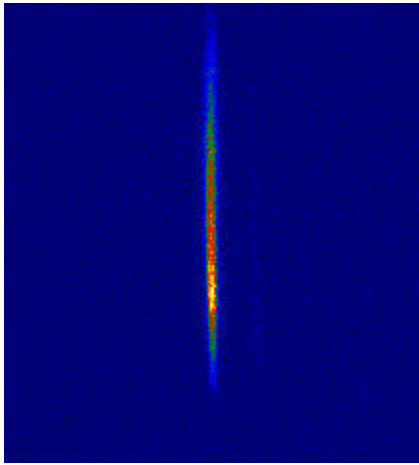


Loading and counting individual
neutral Rb atoms

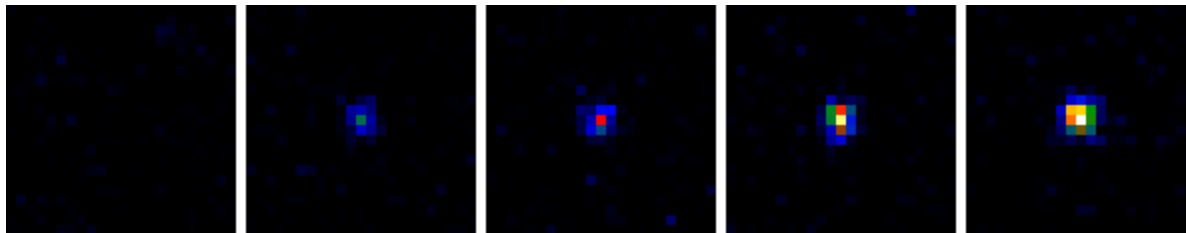
Looking for **single** trapped atoms

Flourescence in a MOT





~10,000 atoms in a lattice
P = .9W, 1.2mK frame is ~.25mm long



0

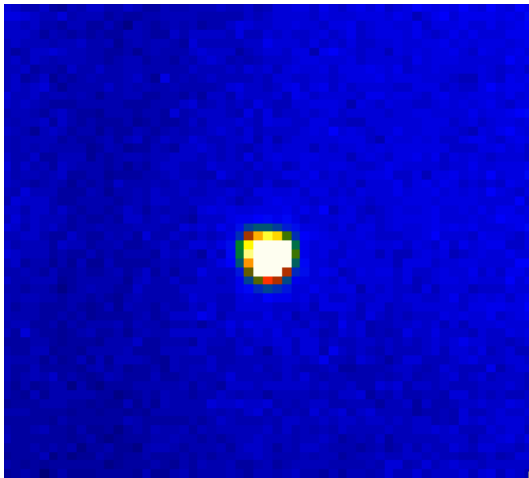
1

2

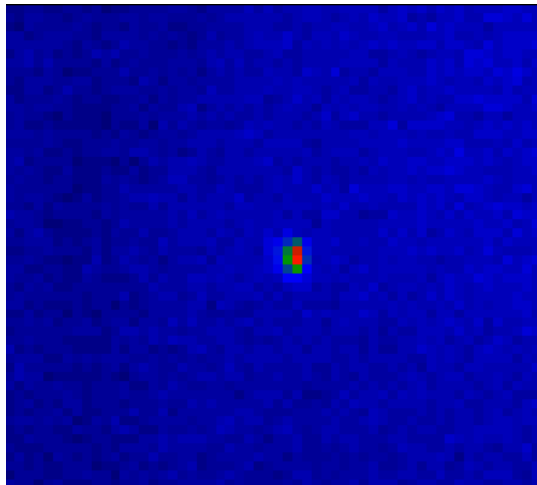
3

4

Imaging Atoms in Optical Lattice



6 atoms in MOT



3 atoms transferred into
lattice

Using a 6 beam MOT with balanced radiation pressure we are able to image the atoms directly in the Optical Lattice

FORT

$$\lambda = 1064 \text{ nm}$$

$$w_0 = 17 \mu\text{m}$$

$$U = 600 \mu\text{K}$$

IMAGING in FORT

Exp time = 1.5 s

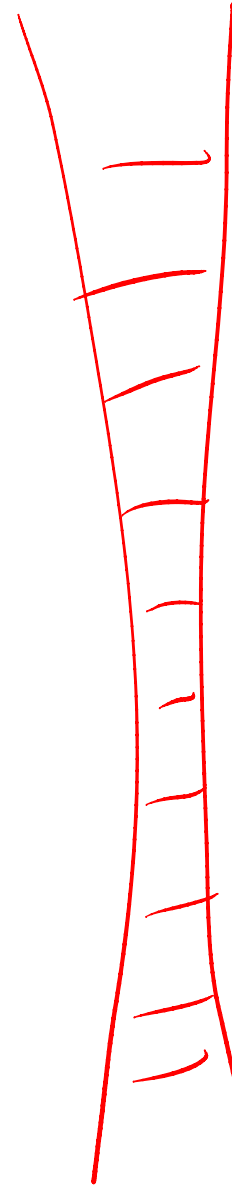
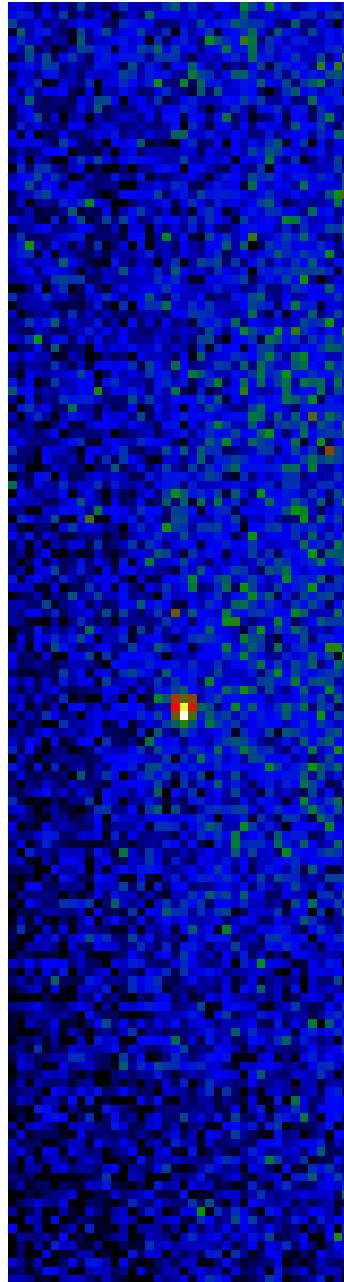
s = 0.0061 per beam

Count rate = 2700/s

Really new data

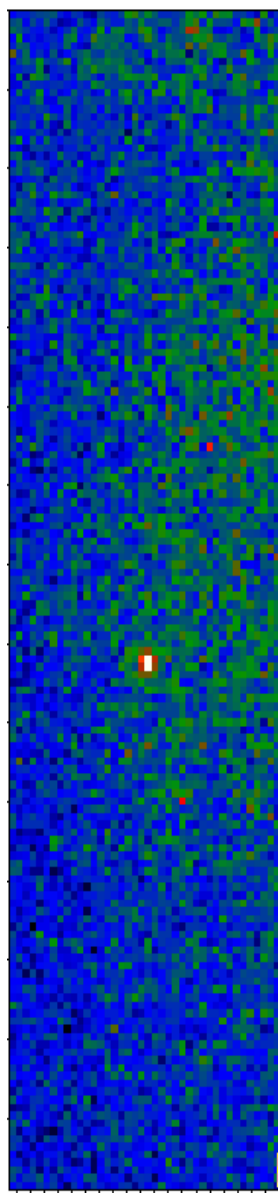
0.5 sec
frame

MOT
location

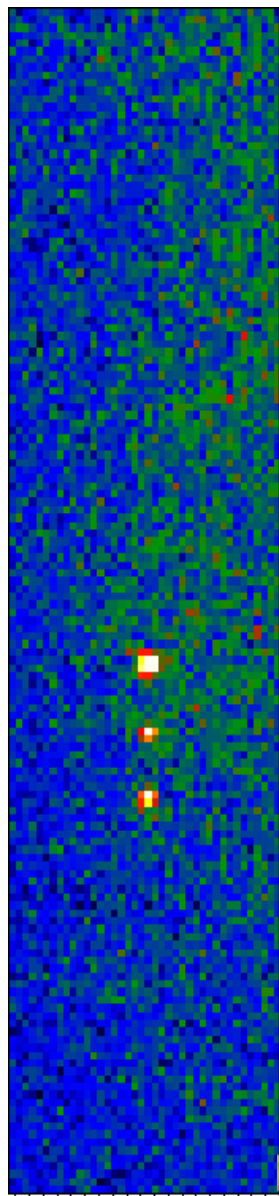


10 am
Mountain
Time
Today

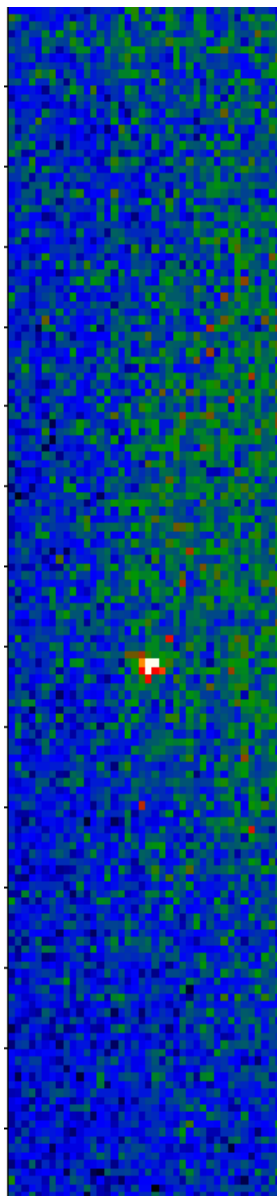
YAG lattice



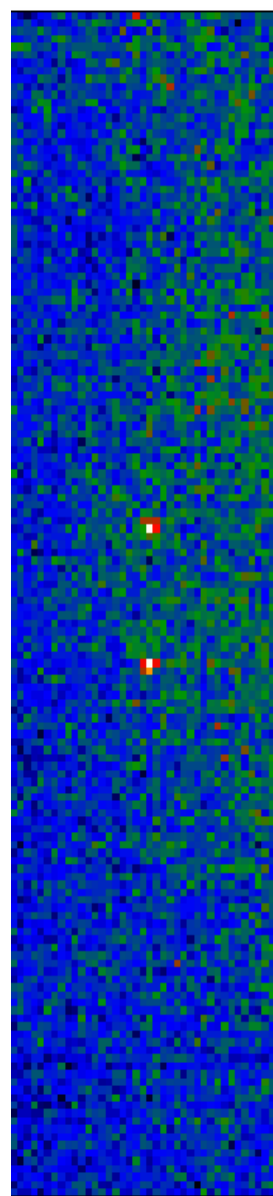
Atoms in
MOT



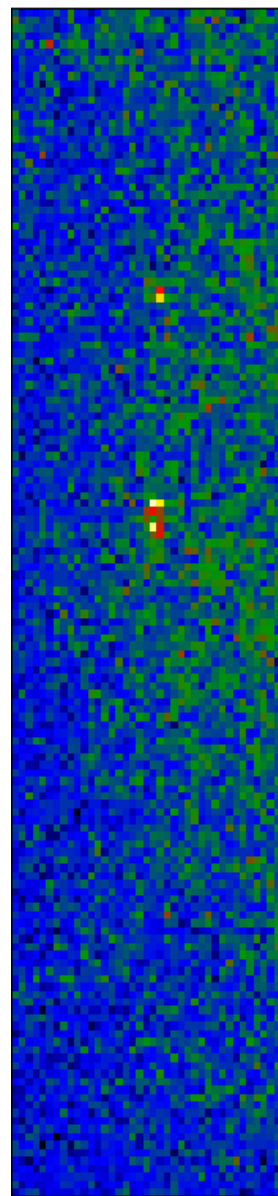
MOT Coils
Turned off
 $t=0$



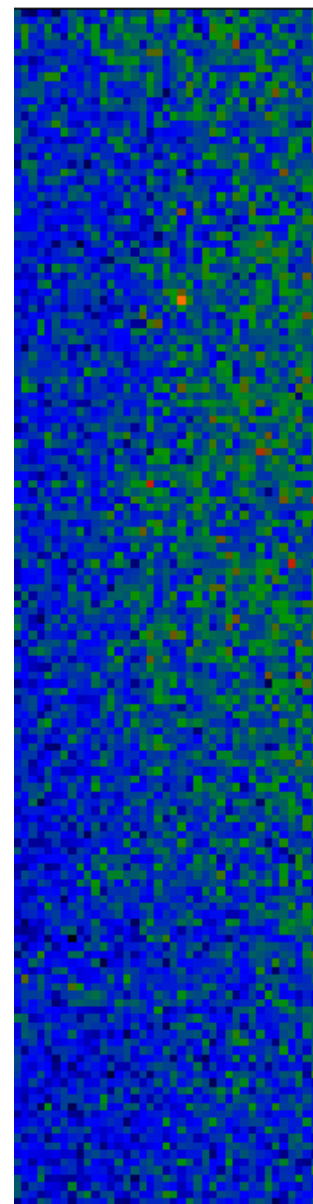
Atoms in
Dipole trap
 $t=5s$



$t=10s$
 $\Delta x = 170\mu m$

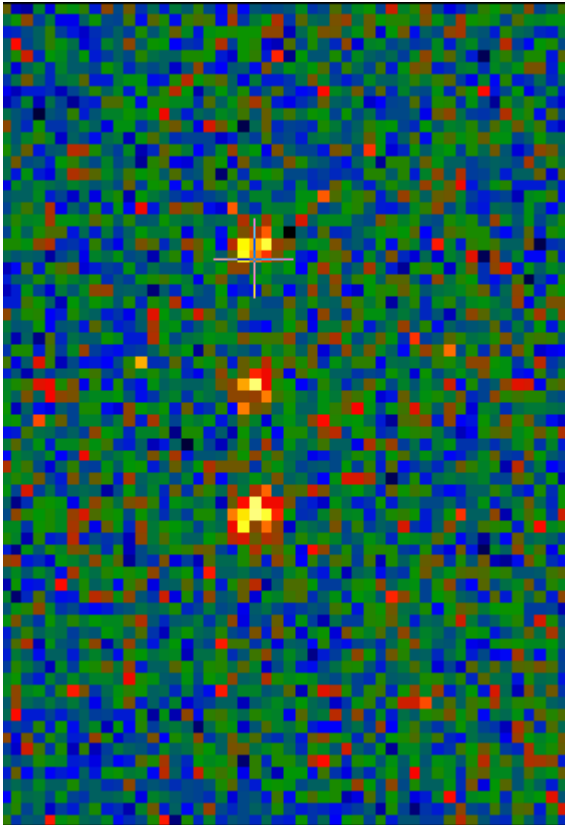


$t=55s$
 $\Delta x = 290\mu m$



$t=244s$

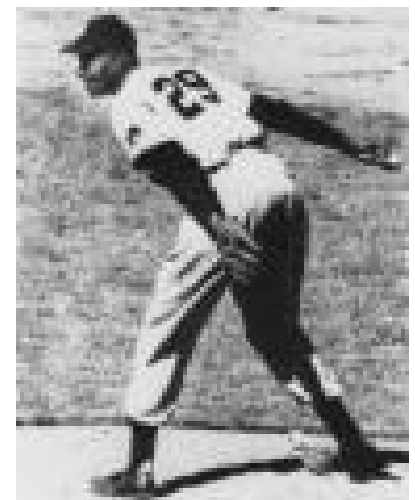
40 mins ago



3 atoms in a row
 $50\mu m$ separation

Don't look back. Something might be gaining on you.

Satchel Paige



ARDA roadmap goals

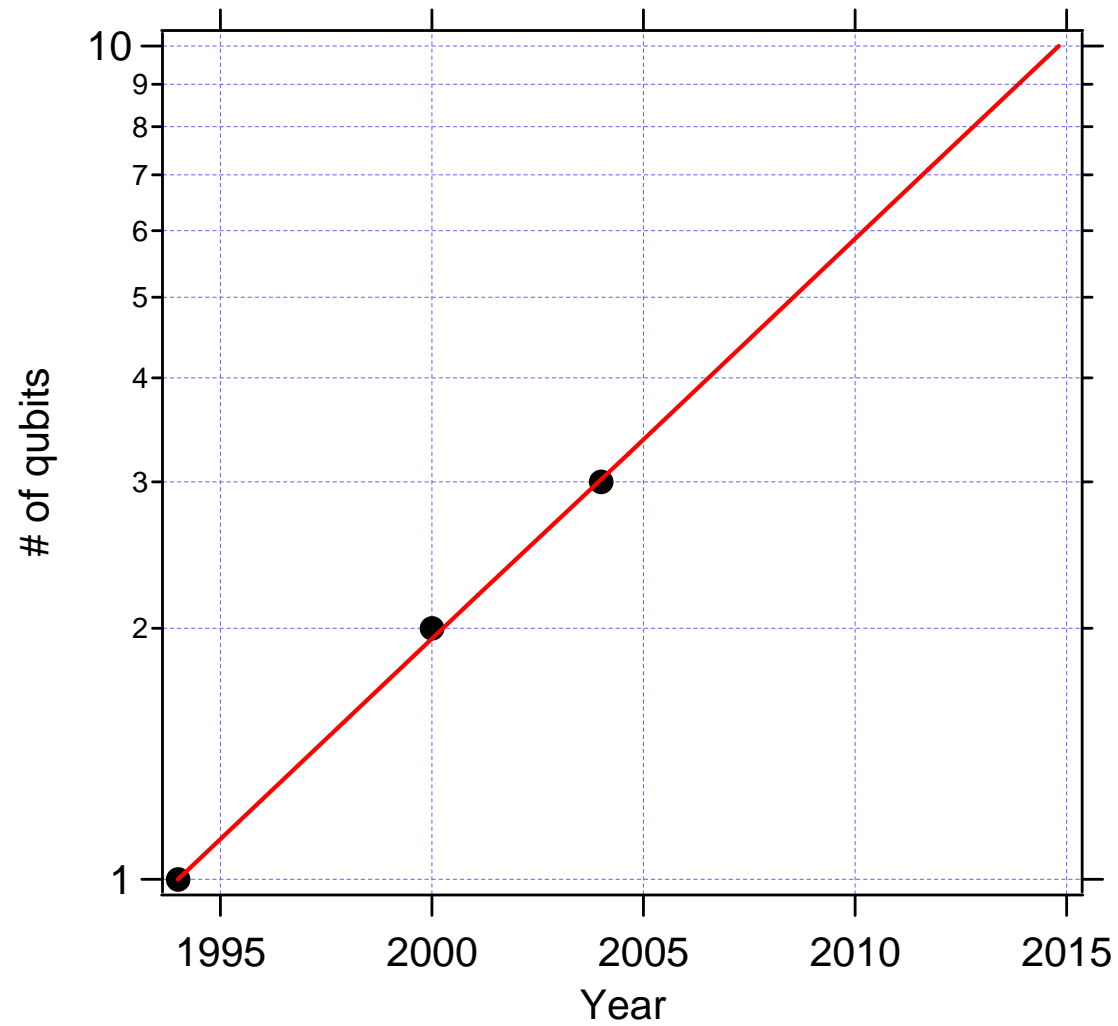
Year 2007 goals (requires ~10 physical qubits)

- encode a single qubit into the state of a logical qubit formed from several physical qubits,
- perform repetitive error correction of the logical qubit
- transfer the state of the logical qubit into the state of another set of physical qubits with high fidelity,

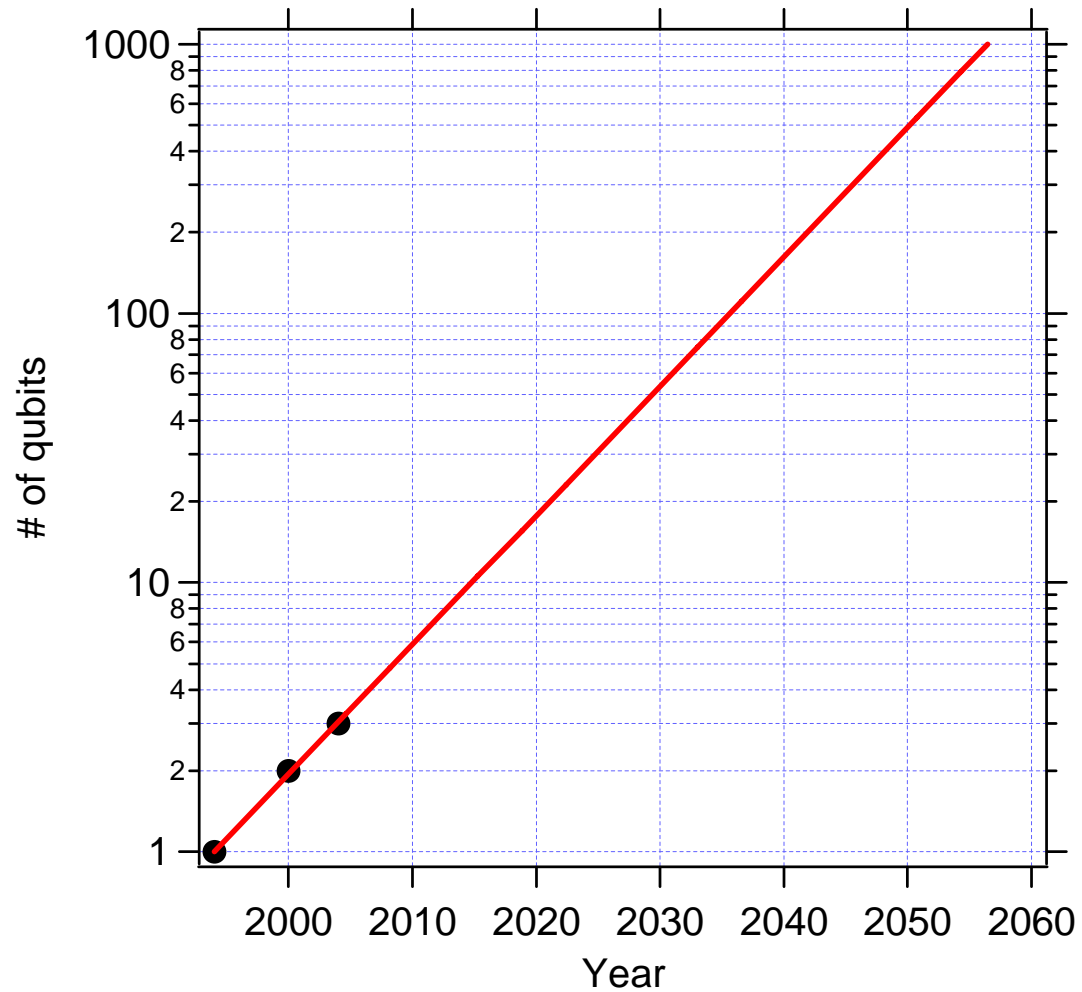
Year 2012 goals (requires ~50 physical qubits)

- implement a concatenated quantum error-correcting code.
- exercise multiple logical qubits through the full range of operations required for fault tolerant QC in order to perform a simple instance of a relevant quantum algorithm

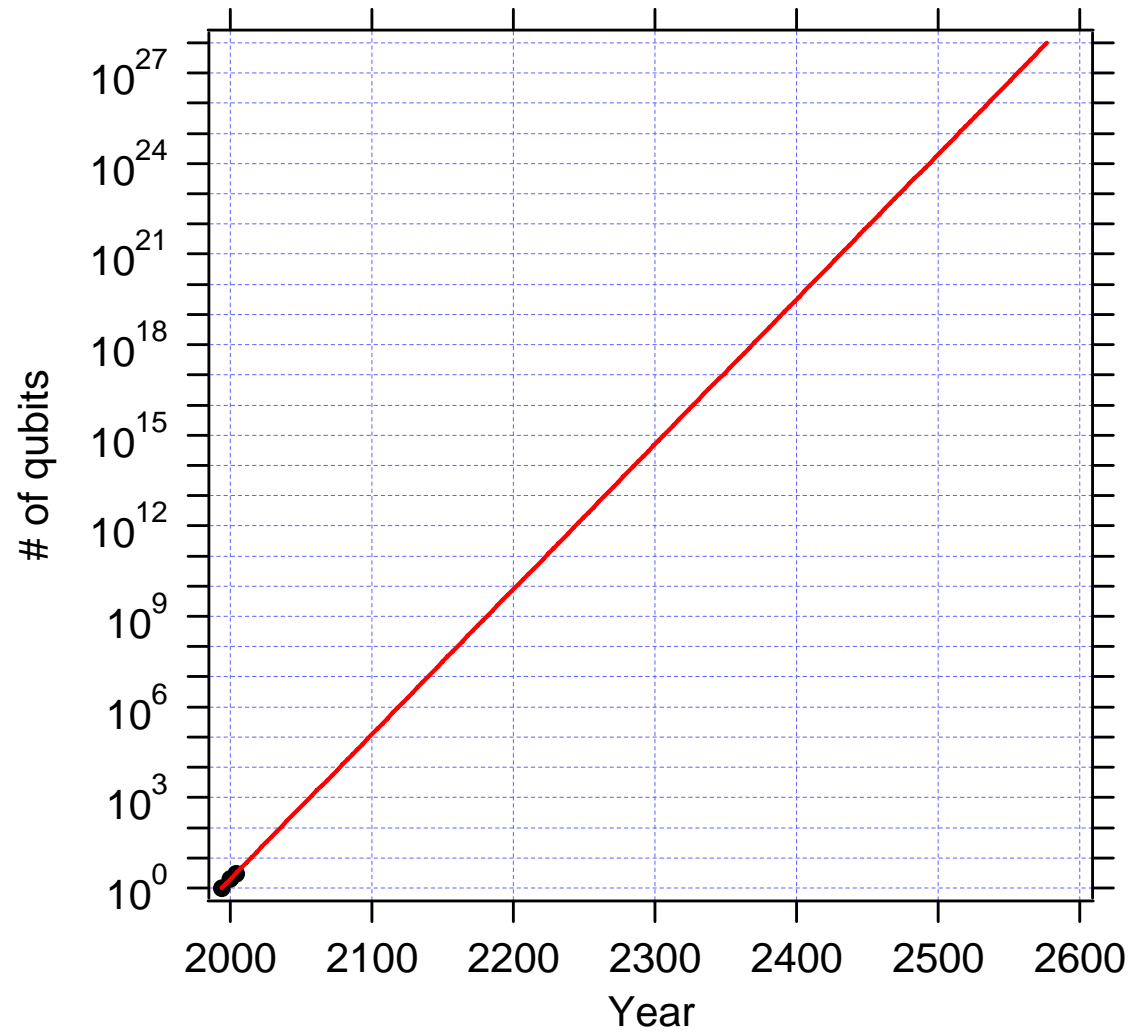
Moore's law for ion traps























































Moore's law for ion traps



Moore's law for ion traps



QC Approach	The DiVincenzo Criteria							
	Quantum Computation						QC Networkability	
	#1	#2	#3	#4	#5		#6	#7
NMR								
Trapped Ion								
Neutral Atom								
Cavity QED								
Optical								
Solid State								
Superconducting								
Unique Qubits	This field is so diverse that it is not feasible to label the criteria with "Promise" symbols.							

Legend:  = a potentially viable approach has achieved sufficient proof of principle
 = a potentially viable approach has been proposed, but there has not been sufficient proof of principle
 = no viable approach is known

- #1. A scalable physical system with well-characterized qubits.
- #2. The ability to initialize the state of the qubits to a simple fiducial state.
- #3. Long (relative) decoherence times, much longer than the gate-operation time.
- #4. A universal set of quantum gates.
- #5. A qubit-specific measurement capability.
- #6. The ability to interconvert stationary and flying qubits.
- #7. The ability to faithfully transmit flying qubits between specified locations.



Adam
Steele

Michael
Gibbins

Qin
Qishu

Kevin
Kortner

Ming Shien
Chang

Nate
Brown

Soo
Kim



Eva Bodjans



Layne
Churchill